Millimeter-wave Base Stations in the Sky: An Experimental Study of UAV-to-Ground Communications

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Abstract—This paper adopts a systems approach to study how millimeter wave (mmWave) radio transmitters on UAVs provide high throughput links under typical hovering conditions. With Terragraph channel sounder units, we experimentally study the impact of signal fluctuations and sub-optimal beam selection on a testbed involving DJI M600 UAVs. From the hovering-related insights and the measured antenna radiation patterns, we develop and validate the first stochastic UAV-to-Ground mmWave channel model with UAVs as transmitters. Our UAV-centric analytical model complements the classical fading with additional losses expected in the mmWave channel during hovering, considering 3-D antenna configuration and beamforming training parameters. We specifically consider lateral displacement, roll, pitch, and yaw, whose magnitude vary depending on the availability of specialized hardware such as real-time kinematic GPS. We then leverage this model to mitigate the hovering impact on the UAV-to-Ground link by selecting a near-to-optimum pair of beams. Importantly, our work does not change the wireless standard nor require any cross-layer information, making it compatible with current mmWave devices. Results demonstrate that our channel model drops estimation error to $\approx 0.2\%$, i.e., 18x lower, and improves the average PHY bit-rate by $\approx 10\%$ when compared to existing state-of-the-art channel models and beamforming methods for UAVs.

Index Terms-mmWave, hovering, UAV-to-Ground, channel model, beam selection

1 INTRODUCTION

The acute spectrum scarcity in the desirable sub-6GHz frequency band has spurred interest in mmWave bands, where substantial amount of untapped channel resources exist [1]. While extensive investigation has been conducted on the particularities of these higher frequencies, the Federal Communications Commission (FCC) is creating new opportunities for the next generation of WiFi in the above-95 GHz band. This has placed mmWave frequencies as a potential candidate to provide high throughput service through the next generation WiFi and 5G standards [2]. Furthermore, from the usage point of view, wireless capacity demand exhibits high spikes of short duration at locations where existing infrastructure may not be sufficient. This makes permanent deployments too costly, forcing to find flexible solutions to cover temporary additional needs. Thus, (i) obtaining a fundamental understanding of the practical constraints of operating in the mmWave bands, as well as (ii) addressing the limitations of static transceiver infrastructure, are salient to realizing a viable mmWave based system [3]. As a possible solution, we envisage a network architecture of UAVs mounted with digitally steerable mmWave antennas, serving as aero mobile base stations, that can be flexibly positioned in time and space.

• Motivation for mmWave-enabled UAV deployment: Given the high capital investment in installing mmWave equipment, static urban deployment must carefully consider cost-benefit tradeoffs, especially when traffic spikes occur at different locations and times. For example, train/bus stations, sporting venues, coffee shops and downtown offices exhibit short-term capacity shortfalls that coincide with human activity patterns [4]. To address these scenarios, UAVs with on-board mmWave radios can be continuously moved to serve pockets of users [5], [6] [7], [8]. In the absence of optical fiber, UAVs rely on point to point mmWave backhaul links to the nearest fixed tower, while serving users on ground (ground nodes) with the desired mmWave cellular or WiFi standard. For our experimental mmWave-enabled UAV channel modeling and beam selection optimization, we have chosen COTS 802.11ad hardware, though our work is applicable to any other mmWave capable WiFi/cellular standard of interest.

• Challenges in mmWave-enabled UAVs: Current mmWave standards use beamforming to create constructive signal addition at the receiver [9], [10]. While beamforming helps combat additional losses due to higher sensitivity to rain/gas absorption and the use of smaller antenna apertures, compared to lower frequencies [11] [12], narrowly directing energy may cause frequent antenna beam misalignments due to the continuous hovering-related UAV displacements. In Fig. 1, we visualize the implications of the term *hovering* as the total sum of various motion artifacts, including translational motion along three axes, and rotational





motion - yaw, roll, and pitch. These types of motion during hovering are caused by the in-built GPS module localization inaccuracy, and follow a Gaussian distribution [13] that can extend up to $\pm 1.5m$ along any single axis in the horizontal plane and $\pm 0.5m$ along the vertical axis within the 3-D space [14], being even larger for less stable UAVs models. In addition to beam misalignment, UAV motion during hovering may lead to an undesirable situation in which the pair of beams chosen by conventional beam selection techniques presents sub-optimal performance over time. We demonstrate this problem in Fig. 2, with actual measured data of the unpredictable UAV displacements. As shown in Fig. 2 (left), when the transmitter and receiver radios are static, the pair of beams selected after beam-sweeping is optimum, resulting in a perfect match over time. However, with hovering UAVs as mmWave transmitters, in Fig. 2 (right), the UAV location fluctuates. As a result of this, the UAV does not statically stay at its initial location, but rather moves from one location to another within the hovering displacement range. Moreover, from our experimental observations, there is no guarantee that when beam-sweeping is performed, the UAV location (Location 1 in Fig. 2), corresponds to the center of the hovering Gaussian distribution (Location 2 in Fig. 2), where the UAV is most likely to be over time. In this case, the selected pair of beams, which was optimum in *Location 1*, turns out to be sub-optimal in average as the UAV location changes and beams become misaligned. The combination of beam misalignment and sub-optimal beam selection eventually lead to received power fluctuations and decreased average performance over time, highly degrading the communication link.

• Summary of Contributions:

Current UAV-to-Ground mmWave channel models are idealistic and limited in their abilities to capture practical effects caused by the UAV airframe and its hovering-related motion. A key unsolved challenge that we tackle in this paper is to design and experimentally validate a fine-grained mmWave channel model that complements the classical fading, by specifically taking into account – (i) the UAV airframe and its effect on the mmWave signal propagation and (ii) fading caused by the unique UAV movement patterns shown in Fig. 1. For the latter, based on experimental observations, we prove that besides expected misalignment loss, hovering motion also causes the sub-optimal beam selection problem discussed in Fig. 2. Non-intuitively, guided by our channel model, our work also demonstrates that choosing specific sub-optimal beams after beam-sweeping,



Fig. 2: Sub-optimal beam selection under hovering

improves the average performance of the UAV mmWavelink over time, compared to the existing standard. Towards this aim, we design an algorithm that optimizes the beam selection for mmWave-enabled UAV transmitters, such that the average SNR at the receiver maximizes over time. To summarize, our work adopts a rigorous systems-approach, by making the following contributions:

(1) We identify and empirically characterize the significant effect of the UAV airframe and the sub-optimal beam selection problem in existing standards using 802.11ad complaint Terragraph radios, in Section 3. In addition, we quantitatively relate these two effects, as well as beam misalignment caused by hovering with, (i) additional fading and (ii) resulting power fluctuations over time, by comparing collected data from static and UAV-to-Ground links.

(2) We build and experimentally validate the first stochastic analytical UAV-to-Ground channel model that takes a systems-approach to estimate additional fading in mmWave links, complementing existing models, in Section 4. In particular, our model includes the effects of UAV translational motion along the three axes, as well as yaw, pitch, and roll characterized from experimental data. Following the acceptance of the paper, the hovering raw data trace-files will be released to the community. Our model also considers the dependence on 3-D radiation patterns of the highly directional antennas, measured under actual flying conditions and potential vibrations. Moreover, and for the first time, we include the effect of a potential sub-optimum beam selection in the fading estimation. Lastly, we tailor our model to different deployment parameters, hovering conditions, and beamforming training configurations, such as the beamsweeping angular resolution and maximum angular range. (3) In order to overcome the problem of sub-optimal beam selection, we propose a standards-compliant approach that selects a near-to-optimum pair of beams for given hovering conditions and antenna radiation patterns, in Section 5.

Moreover, our approach utilizes hovering data collected insitu during actual flight, without using a dedicated time-slot for data collection. We compare our algorithm performance with the standard-based approach during UAV experiments in Section 6, where we also validate our channel model using measured data during flight and show its superior accuracy compared to prevalent idealistic models.

2 RELATED WORK

• Channel Modelling Efforts: There has been a significant effort to understand and characterize mmWave channels in different scenarios over the last few years, including indoor [15], [16], urban [17] and rural environments [18]. The work in [19] presents an overview of channel modeling efforts from several international groups, who propose models for Line-of-Sight (LOS) probability, path loss and building penetration through extensive research and measurement campaigns. Specific to mobility, for Vehicleto-Infrastructure (V2I) communications, the authors in [17] characterize the channel for an urban environment through simulations in the 28 GHz frequency band. For Vehicleto-Vehicle (V2V) communications, an empirical characterization for large and small scale fading is performed in [20], whereas [21] analyzes the effect of small vibrations on the doppler spread. However, none of these works involve UAVs as part of the communication system.

For UAV communications, the works in [22], [23], [24], [25] survey and discuss channel model involving UAVs for the Air-to-Ground link. [22] presents a measurement campaign for both narrow and wide bandwidths, performed in a suburban environment; while [23] proposes a statistical model based on ultrawideband channel sounding. More recently, the authors in [26] and [27] characterize the UAVto-ground channel in LOS and NLOS urban environments through ray tracing simulations, whereas in [28], the authors propose and validate through empirical analysis their proposed Air-to-Ground channel model, without including the unique UAV structural characteristics and hovering motion patterns. However, all these works are developed for the sub-6GHz band, and thus, their outcomes cannot be generalized for higher mmWave frequencies. In contrast, in this work we provide a model to estimate UAV-related fading, applied to a 60 GHz mmWave link that can be generalized to other frequency bands. Although there exist works on channel modeling for UAV-based mmWave links, they lack experimental validation and most of them do not include the UAV dynamics into the model. For instance in [29], the authors use ray-tracing simulations to model the airto-ground channels in 28 GHz and 60 GHz, whereas in [30], a stochastic geometry based 3-D model that considers the directionality and the random heights of transmitters and receivers is proposed. We instead include the UAV motion patterns modelled from collected data during actual flights, and experimentally validate our approach. The closest work found in the literature is presented in [31]. Here, the authors consider additional losses due to the UAV hovering motion, though their model lacks a straightforward relationship with UAV flying parameters and beamforming training configuration. Moreover, they assume an ideal antenna radiation pattern, limiting their analysis to the main lobe.

Lastly, their proposed model is validated with simulations; thus, lacking experimental validation. We show how some of these assumptions may lead to inaccuracies in the theoretical model when compared to actual experimental data.

• beam selection Algorithms: There exist several works aiming to optimize the process of beam selection. In [32] the authors find the optimal steering direction on IEEE 802.11ad compatible devices, accounting for measured radiation patterns and sweeping only through a subset of probing sectors. InferBeam [33], proposes to model the environment as a 3D grid and use Conditional Random Field to map every discrete point to an optimal antenna sector. In [34] the authors track the channel dynamics to find the best beam under mobility. 3D scene reconstruction has been proposed in [35] from surrounding images of a given user, which is used to train a deep neural network, to predict the optimal mmWave transmit and receive beam indices. The authors in [36] estimate the power delay profile of a sub-6 GHz channel, as inputs for a deep neural network to predict the optimal mmwave beam, bypassing the traditional beam sweeping process. Whereas in [37], the authors propose to learn the optimal beam pair index by exploiting the locations and types of the receiver vehicle and its neighboring vehicles (situational awareness), leveraging machine learning classification and past beam training data. However, none of the existing works identify and address the sub-optimal beam selection problem, in particular to hovering UAVs, which we tackle here. To the best of our knowledge, we are the first to provide a robust channel model for mmWave-enabled UAVs that accurately estimates additional fading induced as an effect of realistic antenna radiation patterns, displacement due to UAV hovering, and sub-optimal beam selection. Also, we provide a near-tooptimum beam selection which enhances the average performance under hovering conditions.

3 STUDY OF UAV HOVERING IN MMWAVE LINKS

We first present our hardware selection in Section 3.1. Then, we experimentally characterize the effect of the UAV airframe and the UAV motion during hovering illustrated in Fig. 1, on additional fading compared to static links, in Sections 3.2 and 3.3. Finally, based on our empirical results, we motivate the need for a tailored UAV-to-Ground channel model and improved beam selection algorithm for hovering scenarios, in Section 3.4.

3.1 Hardware Selection

1) *MmWave Sounders.* We use Terragraph (TG) channel sounders, a customized pair of nodes from Facebook [38]. They are designed for the channel modeling of 60GHz links, with capability to measure directional path loss, Signal-to-Noise Ratio (SNR) at the receiver and physical (PHY)-bitrate, among other parameters. Their maximum Effective Isotropic Radiated Power (EIRP) is 45 dBm. Each TG sounder antenna consists of a phased array composed of 36×8 radiating elements. All radiating elements in a given column are connected to the same phase shifter, and thus, steering is not supported in the elevation plane (φ). In the azimuth plane (θ), the steering angular range is [-45° , 45°]. Azimuth steering is performed



Fig. 3: System diagram for the experimental setup

using pre-calibrated antenna weight vectors (AWVs). However, in the existing version of the TG sounders, AWVs cannot be customized, and beam steering is instead achieved using a set of 64 predefined beams. Each predefined beam is a steered version of a uniformly illuminated array. The antenna 3-dB beamwidth (θ_{3dB}) can be set to 2.8°, 8.5°, and 105°. The TG sounders implement the PHY layer of 802.11ad protocol, consisting of 58.32, 60.48 and 62.64GHz frequency bands and MCS of 1 - 12. In 802.11ad, the communicating nodes agree on the optimal pair of transmit and receive beams to maximize signal quality and throughput. This process, referred to as *beamforming training*, takes advantage of the discretized antenna azimuth that reduces the search space of possible antenna array configurations. In the standard, after a first sector matching, a second beamsweeping stage allows further refinement within the selected sectors. TG sounders skip the first sector matching of the 802.11ad beam selection process, and only perform the refinement stage among the set of predefined beams.

- 2) UAV model. Given the total weight (12 Kg) including external modules - the channel sounder and positioning system –, the DJI-M600 is the only apt choice for us, as it can carry weights up to 15 Kg. The UAV is equipped with an in-built GPS module to determine its location and take required actions to reach its targeted coordinates. However, classical in-built GPS module introduces an error of ≈ 0.7 m and up to 1.5 m in the measured location. Thus, when a UAV is programmed to hover at certain targeted coordinates, it experiences a continuous motion around them, as it relies on inaccurate GPS signals for localization. Given this, we also equip the UAV with an RTK-GPS [39], mounted on the M600 as an add-on module and provides a near-stable UAV location measurement with ≈ 0.1 m variation. However, this enhanced positioning accuracy effectively doubles the cost of the M600 setup [39] [40] and hence, our experimental study involves both configurations. The UAV is provided with an Inertial Measurement Unit (IMU) for rotational data collection. An on-board NVIDIA Jetson TX2 compute module stores all sensor data during the experiment.
- 3) Localization measurement system. Our proposed beam selection algorithm requires to log the UAV location during flight with high accuracy. Given the high cost of the M600 RTK-GPS add-on module, we do not assume its



Fig. 4: Antenna radiation pattern under flying conditions

availability. Instead, we use a low-cost RTK-GPS system, EMLID Reach M+, which also provides cm-level localization accuracy. In our setup, this system is only used for data collection and cannot be directly integrated with the UAV navigation system to modify the UAV flight pattern. Thus, three different localization system are mentioned in this work: GPS or RTK-GPS used for navigation and the low-cost RTK-GPS EMLID Reach M+ with the only purpose of data collection.

In Fig. 3, we present a system diagram showing the interconnection between the aforementioned hardware modules.

3.2 Effect of UAV Airframe on the Antenna Radiation Pattern

It is well-known that mmWave signals present reflective properties to certain types of material, such as metal and hard plastic. Moreover, mmWave signal propagation has been proven to be sensitive to potential vibrations induced by wind bursts [41] or by a lack of perfect synchronization in UAV quad-rotor systems [42]. While the aforementioned reflecting materials are commonly used for UAV manufacturing, vibrations can cause UAV instability and alter the antenna frequency response. For this reason, and given the proximity of the mmWave sounder to the UAV underside (see Fig. 6), we were motivated to study how the UAV airframe and potential vibrations affect signal propagation. In order to analyse this phenomena, we compare the TG sounder antenna radiation pattern measured in a RF anechoic chamber for two different setups – (i) with the transmitter on a tripod and thus, free of surrounding reflecting structure, and (ii) with the transmitter attached to the underside of a M600 UAV using 3-D printed hardware, as we illustrate in Fig. 6. For the latter setup, the UAV rotors were turned on, in order to account for vibrations and emulate flying conditions as closely as possible. We denote these setups as static and aerial, respectively. The receiver remained on a tripod in both setups, at a height of 1.5 meters above the ground, 6 meters away from the transmitter. For each setup, we characterized the radiation pattern for the central beam at the transmitter, according to the predefined beams mentioned in Section 3.1. To this extent, we made both TG sounders perfectly face each other, and fixed their central beams for transmission and reception. Then, we rotated the transmitter sounder by angular steps of 1°, so that the beams were steered away from each other at an azimuth angle $\theta \in \mathbb{Z}$

in the range [-30, 30] ($\theta = 0^{\circ}$, being the perfect alignment). For each position, we logged the link path loss and calculated the electric field from $E(dB/m) = 10log(\sqrt{Z_0P_d})$, where Z_0 is the free space impedance equal to 120π , and P_d is the power density, computed as $P_d = \frac{gP_r}{4\pi d^2}$, with g the antenna gain, d the distance between transmitter and receiver and P_r the received power calculated as the difference between the EIRP set for transmission and the measured path loss. For validation, we contrasted our characterization for the first setup (tripod case) with TG documentation.

In Fig. 4, we present the measured radiation patterns for both setups, and observe the effect the UAV airframe has on its shape. For reference, we additionally include the *ideal* radiation pattern calculated from antenna array synthesis, for the same beamwidth θ_{3dB} of 2.8° as for the experimental characterization. From the comparison between the static and *aerial* radiation patterns, we observe that the UAV hardware and its in-motion rotors cause additional fading L_{Afr} of 9.5 dB, as they perturb the mmWave electric field in the near-field region. Specific values for L_{Afr} depend on the amount of power reflected and scattered on the UAV airframe, given by (i) the UAV airframe shape and material, (ii) the antenna radiation pattern, and (iii) the sounder assembly on the UAV. For our case, since TG sounders do not perform elevation steering, significant amount of power is reflected on the UAV underside, causing large additional fading. Under this observation, theoretical models need to consider potential hardware-mounting related fading in practical deployments.

3.3 Effect of UAV Hovering on the Link Performance

In this section, we aim to experimentally quantify the link performance degradation caused by UAV hovering-related motion, and illustrate its dependency with different deployment and system configuration parameters. To this extent, we first describe in Section 3.3.1 the two direct effects caused by hovering - beam misalignment and potential sub-optimal beam selection -, already introduced in Section 1. Then, in Section 3.3.2, we quantify through experiments how these two phenomena result in power fluctuations and additional fading when compared to static deployments.

3.3.1 Understanding Hovering-Related Effects

First, we illustrate the origin of power fluctuations due to beam misalignment by referring to Fig. 5a. Initially, right after the beam-sweeping procedure, transmitter, and receiver beams are perfectly aligned. However, as the transmitter UAV suffers from hovering and experiences displacement from its initial location, its beam becomes misaligned with the receiver's. This causes additional loss L_{Misal} compared to a static setup, as the antenna gains drop. Since the displacement is due to hovering, that is of unpredictable nature, the antenna gains, and consequently L_{Misal} , randomly fluctuate over time. Moreover, the fluctuations magnitude is highly dependent on the antenna radiation patterns and hovering conditions according to Fig. 5a, and increases as the distance between transmitter and receiver is reduced. This highlights the importance of carefully considering hardware features for loss estimation, such as the antenna



Fig. 5: Illustrating the hovering-related fading caused by (a) beam misalignment and (b) sub-optimal beam selection

characteristics and the accuracy of the system used for UAV navigation, which conditions its stability during hovering.

In Fig. 5b, we show the result of sub-optimal beam selection after completing the 802.11ad standard beam-sweeping procedure, caused by the lack of accuracy of the in-built GPS module, as we discussed in Fig. 2. The selection of a suboptimal pair of beams has two consequences. First, it causes misalignment loss at the center of the hovering displacement range, where the UAV is more likely to be located over time. We denote this loss as L_{SubOpt} , in order to distinguish it from the temporal varying loss discussed in Fig. 5a. Furthermore, as the transmitter hovers under sub-optimal beam conditions in Fig. 5b, the magnitude of the L_{Misal} fluctuations would likely change, as the displacement of UAV would produce misalignment along different regions of the radiation patterns compared to the case in Fig. 5a, causing the antenna gains to also vary on a different range of values. This fact reveals the dependence of L_{Misal} with the selection of a particular pair of beams after beam-sweeping, highlighting the need to jointly consider both effects. The selection of a certain pair of beams is determined by the UAV hovering conditions, distance between transmitter and receiver and antenna radiation patterns. In addition, it also depends on the beamforming training parameters, which determine the angular direction to which transmitter and receiver steer their beams during beam-sweeping.

3.3.2 Quantifying Hovering Effect on Link Performance

In order to quantify the effect of hovering-related loss on the link performance, we conduct a set experiments. We consider three scenarios experiencing different degree of hovering: a static Ground-to-Ground link, a UAV-to-Ground link where the UAV navigation system relies on an in-built GPS localization module, and the same UAV-to-Ground link where the GPS is replaced by an RTK-GPS module, for increased localization accuracy, as we discussed in Section 3.1. We show our experimental setup in Fig. 6 for the UAV-to-Ground case. It consists of a 802.11ad compliant TG sounder unit mounted on a DJI-M600 UAV operating as a transmitter and another TG sounder unit mounted on a tripod operating as the ground receiver. For the Ground-to-Ground link, both

IEEE TRANSACTIONS ON MOBILE COMPUTING

TABLE 1: SNR (dB) for Different Confidence Levels

Type of Link	25%	50%	75%
Ground-Ground (Static)	18.2	18.7	19
UAV-Ground (Hovering, GPS)	17	17.4	17.9
UAV-Ground (Hovering, RTK-GPS)	5	7.5	10.5

sounders are mounted on tripods. For these experiments, we collect link path loss and SNR by connecting the transmitter and receiver sounder units to a host computer through Ethernet links, as illustrated in Fig. 3, which are long enough so that we do not compromise the UAV natural hovering pattern. We fix the beamwidth θ_{3dB} to the narrowest achievable by TG sounders with its current firmware of 2.8°, motivated by a longer communication range compared to wider beamwidths. However, the general trends can be extrapolated to other beamwidths. As the overlay protocol used is 802.11ad, the best transmitter-receiver beams are automatically selected as per the standard.

In Fig. 7a we show the path loss collected over time for all three scenarios considered. These measurements capture the cumulative fading arising from the two hovering-related effects discussed in Section 3.3.1, as well as the fading caused by the UAV airframe quantified in Section 3.2, none of which apply to the static Ground-to-Ground case. We first observe that the path loss for the UAV-to-Ground link using RTK-GPS only differs from the static case by a magnitude equivalent to the measured airframe fading of 9.5 dB. This is due to the scarce hovering experienced by the UAV when its navigation system relies on RTK-GPS, which limits the severity of power fluctuations caused by beam misalignment, as well as the chances for sub-optimal beam selection after beam-sweeping completion. In order to prove that the observed power fluctuations are due to beam misalignment, we rely on the knowledge of the antenna radiation pattern. We observe that for a typical maximum hovering translational displacement along y-axis Δ_y and for a given distance between transmitter and receiver d, we can determine the maximum angular displacement in the azimuth dimension $\Delta_{\theta} = atan \frac{\Delta_y}{d}$. Then, from the antenna radiation pattern, we can estimate the gain fluctuation within the range $[-\Delta_{\theta}, \Delta_{\theta}]$, which is bounded by 6 dB for the RTK-GPS case, where $\Delta_v \approx 0.1$ m and d = 6m in our setup. We observe that the gain fluctuation matches the experimental power fluctuation magnitude in 7a. Notice that fading is aggravated when the UAV relies on GPS for navigation and thus, suffers from worse hovering conditions. In this case, the fluctuating path loss values collected during the entire experiment time are bounded by 14 dB, which also matches our estimation based on the antenna radiation pattern. Moreover, these fluctuations are at least 15 dB above the case using RTK-GPS. Therefore, we associate this loss gap to the direct consequence of a sub-optimal beam selection, as choosing a specific pair of beams determines the region of the radiation pattern along which the UAV hovering causes beam misalignment, which may lead to the case in which sub-optimal pairs never reach perfect alignment. These results confirm our hypothesis that the navigation system lack of accuracy causes hovering, eventually leading to increased fading compared to static setups. In Fig. 7c we show the Empirical Cumulative Distribution Function (ECDF) of the measured SNR for the same experiment and



Fig. 6: Experimental setup and close-up view of M600 (inset) with TG sounder and RTK-GPS unit

all three scenarios considered. The SNR for different confidence level is provided in Table 1. Based on the 802.11ad protocol [43], the SNR for a GPS-based system maps into a PHY-bitrate drop of 17% with probability 50% and a drop of 33% with probability 25% compared to static Ground-to-Ground links.

3.4 Summary and Discussion

Below, we highlight the main take-away points from this experimental study that we will directly leverage in our channel model and beam selection algorithm:

- Hovering introduces significant path loss in mmWave bands for highly directional, narrow beamwidths. This loss is dependent on the extent of hovering-related motion artifacts, the antenna radiation patterns, and the possibility of an initial sub-optimal beam selection. This, together with the observed effect the UAV airframe has on signal propagation, motivates the need to create a channel model with a systems-driven approach that can be tailored towards different antenna configurations and UAV hovering characteristics.
- Existing standards for mmWave communication, such as the 802.11ad, are not optimized for best beam alignment in UAV links, and lead to a persistent performance degradation over time. Thus, we need to design a custom beam selection algorithm, which is able to make a better selection at the end of the regular beam-sweeping phase, without modifying the standard.

4 MMWAVE CHANNEL MODEL FOR UAV LINKS

In this section, we first determine where our contributions are within the channel modelling framework in Section 4.1, where we also discuss the most relevant known results that are leveraged in building comprehensive mmWave models. We then introduce our proposed model in Section 4.2, where we provide a complete estimation of mmWave-band fading that can be applied to multiple UAV hovering scenarios. Table 5 lists all notations and can be found at the end of the document.

4.1 Channel Model Background

In wireless propagation, fading can be classified into large and small scale. Large scale fading accounts for Free



Fig. 7: Showing (a) effect of hovering-related losses on the link performance compared to a static case, (b) polar and Cartesian coordinate systems and beamforming training parameters and (c) SNR drop caused by hovering



Fig. 8: Contribution within the channel model framework

Space Path Loss (FSPL) and shadowing effect. Small scale fading includes rapid fluctuations of the received signal strength over very short distance and time, which is manifest through multipath and doppler effect. Our proposed channel model do not intend to provide a more accurate estimation of these effects, but instead, to complement existing channel modelling efforts to obtain an accurate fading estimation tailored to UAV-to-Ground links. In Fig. 8, we show a diagram with the aforementioned classification into large and small scale fading and the effects belonging to each category. Within this channel modelling framework, we illustrate where our contributions, i.e., UAV airframe and hovering-related effects discussed in Section 3.2 and 3.3 respectively, fit. In particular, we consider airframe loss L_{Afr} as additional large scale fading and hovering-related loss L_{Hov} as small scale fading, as the latter is caused by the UAV change of location around its targeted coordinates over time. In Fig. 8, we also refer to some of the most relevant models in the literature, that can be jointly combined with our work. In particular, for large scale fading, the NYU Rural Macro environments (RMa) model [18] is a suitable option, since it is specifically derived for mmWave frequencies, obtained through extensive measurements in the 73 GHz band, with accompanying experimental validation. Other alternatives such as the 3GPP and ITU-R RMa path loss models were originally derived for the sub-6 GHz band. Regarding small scale fading due to multipath, Nakagami distribution is an accurate model at mmWave frequencies [44]. Finally, additional path loss due to interference generated by doppler spread is given in [31]. However, doppler effect is typically considered negligible for speeds

below 10 m/s, and thus, it is not included for scenarios in which UAVs are hovering at a fixed location.

4.2 Proposed Channel Model for UAV-to-Ground links

In this section, we introduce our proposed stochastic channel model for estimating additional fading specific to UAVbased links, cumulatively caused by the UAV airframe and hovering-related effects discussed in Section 3. In particular, we consider the airframe effect on the radiation pattern, and the losses caused by beam misalignment and sub-optimal beam selection. The proposed model takes multiple input parameters (Section 4.2.1), to be tailored to the system beamforming training configuration, deployment parameters and hardware assumptions, such as antenna features and level of accuracy of the UAV localization system. We then introduce the steps to build the model in Sections 4.2.3-4.2.5, where we estimate misalignment loss, total hovering-related loss, and total link-loss, as well as the probability that they remain below a given threshold, crucial for accurate link-budget estimation and careful deployment planning.

4.2.1 Input Parameters

In order to provide an accurate fading estimation, our channel model takes the following inputs:

- 1) 3-D static and aerial antenna radiation patterns. Our channel model requires both radiation patterns in order to determine additional loss caused by the UAV airframe L_{Afr} in the angular domain. We build the 3-D radiation patterns from 2-D azimuth θ and elevation φ slices of the antenna power distribution. We obtain the 2-D slices from measurements, as we describe in Section 3.2, as well as through antenna array synthesis with limited accuracy (see Fig. 4). Alternatively, if the antenna dimensions are known, 3-D radiation patterns can be directly obtained in simulation, using electromagnetic software packages.
- 2) *UAV motion data during hovering*. We collect UAV motion data during the complete flight time, for all translational and rotational types of motion illustrated in Fig. 1. From this data, we build the UAV hovering statistics in Section 4.2.3. To measure translational data, we use a highly accurate low-cost RTK-GPS (EMLID Reach M+).

- 3) Beamforming training parameters. In particular, we consider the angular range evaluated during beam-sweeping $\Delta_{\theta_{SW}}$, $\Delta_{\varphi_{SW}}$, and the angular resolution $\delta_{\theta_{SW}}$, $\delta_{\varphi_{SW}}$, this is, the angular distance between two consecutive evaluated beams. By considering beamforming training parameters within the model, it is possible to evaluate the effect of different beam-searching reduction techniques extensively proposed in the literature in UAV links, which has been mostly evaluated in static scenarios. We leverage the beamforming parameters and hovering statistics built from the UAV positioning data to estimate the probability for a certain pair of beam to be selected after the beam-sweeping procedure, in Section 4.2.4. This is crucial, as the selection of a particular pair of beams with certain probability, together with the aerial and static antenna radiation patterns, stochastically determine the fading experienced (see Fig. 5).
- 4) *Deployment parameters*, including the distance between transmitter and receiver *d*, directly provided or estimated from the UAV and Ground node localization data. Additional fading such as the caused by unfavorable atmospheric conditions or different types of environment can be easily build into the model, as we next illustrate in Section 4.2.2.

4.2.2 A Systems Perspective for Stochastic Fading Estimation

We start by formulating the total link loss or fading L_{Tot} as:

$$L_{Tot} = L_{FSPL} + L_{Afr} + L_{Hov} \tag{1}$$

where, L_{FSPL} is the Free Space Path Loss, L_{Afr} is the fading caused by the effect of the UAV airframe on the antenna radiation pattern and L_{Hov} comprises all hovering-related fading. We separate L_{Hov} into three terms: fading due to an initial sub-optimal beam selection L_{SubOpt} , fading due to distance variations between transmitter and receiver $L_{\Delta r}$, due to the UAV translational motion along x-axis, and fading caused by beam misalignment L_{Misal} due to translational motion along y and z axes, as well as yaw and pitch.

$$L_{Hov} = L_{SubOpt} + L_{\Delta_r} + L_{Misal} \tag{2}$$

Notice from Fig. 5b that, for a given pair of beams with transmitter and receiver pointing angular directions $\{\theta_T, \varphi_T\}$ and $\{\theta_R, \varphi_R\}$, L_{SubOpt} is deterministic. We use the notation (u, v) to refer to a specific pair of beams with indexes $u \in \mathbb{N}$ in azimuth and $v \in \mathbb{N}$ elevation dimensions. A deterministic behaviour also applies to L_{FSPL} and L_{Afr} , since the distance *d* variability during hovering is included in L_{Δ_r} , as part of L_{Hov} , and assumed to be constant for the L_{FSPL} estimation. Thus, by considering the deterministic nature of the aforementioned factors, and noticing that for a fixed pair of beams, $L_{Misal}|_{(u,v)}$ and L_{Δ_r} are the only stochastic terms, we estimate the probability for a given total link fading $L_{Tot}|_{(u,v)}$ as follows:

$$P(L_{Tot}|_{(u,v)}) = P(L_{\Delta_r} + L_{Misal}|_{(u,v)})$$
(3)

Where the sum between $L_{\Delta r}$ and $L_{Misal}|_{(u,v)}$ is related to the total link fading $L_{Tot}|_{(u,v)}$ according to Eqs.(1) and (2):

$$L_{\Delta_r} + L_{Misal}|_{(u,v)} =$$

$$L_{Tot}|_{(u,v)} - L_{FSPL} - L_{Afr} - L_{SubOpt}|_{(u,v)}$$
(4)

8

Notice that Eq.(3) assumes the selection of a *given pair* of beams. Therefore, the probability for the UAV-to-Ground link to experience a certain total fading $P(L_{Tot})$ considering *all possible pairs* of beams which are candidate to be selected after the beam-sweeping procedure, depends on (i) the probability for a given pair of beams (u,v) to be selected after the beam sweeping procedure, denoted as P(u, v), as well as (ii) the probability for the link to experience the loss calculated from Eq.(4), denoted as $P(L_{\Delta_r} + L_{Misal}|_{(u,v)})$:

$$P(L_{Tot}) = \sum_{u,v} P(u,v)P(L_{\Delta_r} + L_{Misal}|_{(u,v)})$$
(5)

With $\sum_{u,v} P(u,v) = 1$.

Then, the estimated average total link fading is given by:

$$\overline{L_{Tot}} = L_{FSPL} + L_{Afr} + \overline{L_{Hov}}$$
(6)

With $\overline{L_{Hov}}$ the average hovering-related fading:

$$\overline{L_{Hov}} = \overline{L_{\Delta_r}} + \sum_{u,v} (L_{SubOpt}|_{(u,v)} + \overline{L_{Misal}}|_{(u,v)}) \cdot P(u,v) \quad (7)$$

We derive each term in the next sections. Here, we first remark the systems approach taken by this model, as it considers hardware-related loss, as well as beamforming training and deployment parameters. Moreover, the model provides flexibility to include any additional classical fading which is relevant to the scenario under analysis, such as those referenced in Fig. 8. This can be achieved by simply replacing the term L_{FSPL} by more accurate estimations, which include additional fading effects such as shadowing or unfavorable weather conditions, or by directly adding new terms into Eq.(1).

4.2.3 Modeling Motion of Hovering UAVs

The first step towards building our UAV-to-Ground channel model, is to determine the hovering-related loss L_{Hov} . This, together with L_{Afr} , already characterized in Section 3.2, represent fading particular to UAV-links. To this extent, we statistically model all types of UAV motion during hovering and build each motion distribution, similar to the one we show for a single type of motion in Fig. 2. Recalling Fig. 1, hovering motion manifests in longitudinal, lateral, and vertical translational displacements along (x, y, z) axes, as well as rotational displacements around them, respectively, denoted as *roll*, *pitch*, and *yaw*.

It is important to notice that not all types of motion are independent from each other. For instance, UAV translational displacement along the negative side of y-axis $-\Delta_{y}$, can be compensated by positive rotational displacement around z-axis $+\Delta_{yaw}$. Similar dependency exists between Δ_z and Δ_{pitch} . For this reason, it is desirable to define UAV displacements in a coordinate system which enables to jointly combine the effect of different types of motion. We select the polar coordinate system (r, θ, φ) , where $r \equiv x$, $\theta \equiv yaw$ is the rotational dimension in the plane XY, and $\varphi \equiv pitch$ is the rotational dimension in the plane YZ, see Fig. 7b. Moreover, with the selection of the polar coordinate system, we directly relate UAV displacements with the antenna radiation pattern, naturally characterized in azimuth θ and elevation φ , required for estimating hoveringrelated loss. The distance between transmitter and receiver is defined along dimension r. In Table 2, we provide the conversion from UAV to polar coordinates, according to

TABLE 2: UAV to Polar Coordinates Conversion

Polar Coordinates	UAV Coordinates Projection over (r, θ, φ)
Δ_r	$\begin{split} \Delta_{r_{(x)}} &= \Delta_x \\ \Delta r_{(y)} &= \sqrt{(\Delta y)^2 + d^2} - d \approx 0 \\ \Delta r_{(z)} &= \sqrt{(\Delta z)^2 + d^2} - d \approx 0 \\ \Delta r_{(roll)} &= \Delta r_{(pitch)} = \Delta r_{(yaw)} = 0 \end{split}$
Δ_{θ}	$\begin{split} \Delta_{\theta_{(y)}} &= atan(\frac{\Delta_y}{d})\\ \Delta_{\theta_{(yaw)}} &= \Delta_{yaw}\\ \Delta_{\theta_{(x)}} &= \Delta_{\theta_{(coll)}} = \Delta_{\theta_{(pitch)}} = 0 \end{split}$
Δ_{φ}	$\begin{split} \Delta_{\varphi_{(z)}} &= atan(\frac{\Delta_z}{d})\\ \Delta_{\varphi_{(pitch)}} &= \Delta_{pitch}\\ \Delta_{\varphi_{(x)}} &= \Delta_{\varphi_{(y)}} &= \Delta_{\varphi_{(roll)}} = \Delta_{\varphi_{(yaw)}} = 0 \end{split}$

TABLE 3: Variance of Hovering Displacement

Navigation system	$\sigma^2_{\Delta_x}$	$\sigma^2_{\Delta_y}$	$\sigma^2_{\Delta_z}$	$\sigma^2_{\Delta_{roll}}$	$\sigma^2_{\Delta_{pitch}}$	$\sigma^2_{\Delta_{yaw}}$
GPS	0.0586	0.035	0.0582	0.1968	0.1876	0.0027
RTK-GPS	0.0032	0.0021	0.0033	0.1415	0.1139	0.0028

Fig. 7b. The notation $\Delta_{i(j)}$ represents the projection of the hovering displacement for the UAV coordinate *j* over the polar dimension *i*. Accordingly, hovering displacements in polar coordinates are given by:

$$\Delta_r \approx \Delta_x \tag{8}$$

$$\Delta_{\theta} = \Delta_{\theta_{(y)}} + \Delta_{yaw} = atan(\frac{\Delta_y}{d}) + \Delta_{yaw}$$
(9)

$$\Delta_{\varphi} = \Delta_{\varphi(z)} + \Delta_{pitch} = atan(\frac{\Delta_z}{d}) + \Delta_{pitch}$$
(10)

In order to characterize the UAV motion comprehensively, we collect experimental hovering data during flight for all six types of motion in Fig. 1. We perform our experiments under typical hovering conditions, i.e., scenarios with no buildings within a radius of 15 meters, strong satellite signal reception (SNR >35 dB) from at least 4 satellites, and maximum wind speed of 17 miles/hour, which are conducive for safe and reliable operation. We measured translational displacement in (x,y,z) coordinates with two different hardware configurations, for the M600 UAV navigation system relying on (i) GPS and (ii) a high-cost RTK-GPS, which limits the UAV maximum hovering displacement, and thus, its variance. For both configurations, we used a separate low-cost RTK-GPS system, mounted on the UAV with the only purpose of accurate data logging, not interacting with the UAV navigation system; thereby, not affecting its flight pattern. For both configurations, we collected rotational displacement data using IMU sensors.

Figs. 9a and 9b show the distribution of the experimental data collected for Δ_y and Δ_{yaw} respectively, as examples. From the experimental data collected, we observe that UAV displacements during hovering follow a Gaussian distribution in each UAV coordinate *j*:

$$\Delta_j \sim \mathcal{N}(\mu_{\Delta_j}, \, \sigma_{\Delta_j}^2) \tag{11}$$



Fig. 9: Gaussian distribution of UAV (a) translational displacements in y-axis and (b) rotational displacement in yaw

where $\sigma_{\Delta_j}^2$ represents the variance of the displacement and μ_{Δ_j} its mean value, tending to the targeted coordinates at which the UAV ideally should be located. Placing the origin of the UAV coordinate system at the targeted coordinates, we set $\mu_{\Delta_j} = 0, \forall j$ for simplicity. In Table 3, we provide specific values for the variance of the data collected. The hovering statistics used in this work are not pre-determined and fixed. Instead, we build these statistics from measurements collected during live deployment, as UAV hardware choices, and operating conditions may be different for specific use cases.

Next, from the characterization performed in UAV coordinates, we build the hovering distribution in polar dimensions. According to Eq.(8), the probability density function (PDF) for the displacement in the radial dimension $f_r(\Delta_r)$ is approximated by the Gaussian PDF of the longitudinal displacement $\Delta_x \sim \mathcal{N}(0, \sigma_{\Delta_x}^2)$. Moreover, according to Eq.(9), the PDF for the displacement in the azimuth dimension $f_{\theta}(\Delta_{\theta})$ needs to consider the combined effect of *yaw* as well as the projection over θ of the translational displacements along y-axis $\Delta_{\theta(y)}$. We define the unnormalized distribution for the azimuth displacement as:

$$f_{\theta_{\mathcal{U}}}(\Delta_{\theta}) = \int_{-\pi}^{\pi} \int_{-\pi}^{\pi} f(\Delta_{\theta_{(y)}}) f(\Delta_{yaw})$$

$$\delta(\Delta_{\theta} - \Delta_{\theta_{(y)}} - \Delta_{yaw}) d_{\Delta_{yaw}} d_{\Delta_{\theta_{(y)}}}$$
(12)

where $f(\Delta_{\theta_{(y)}})$ and $f(\Delta_{yaw})$ are the independent Gaus-

sian PDFs of $\Delta_{\theta_{(y)}}$ and Δ_{yaw} respectively, and δ is the Dirac delta function:

$$\delta(\Delta_{\theta}) = \begin{cases} 1, & \text{if } \Delta_{\theta} = \Delta_{\theta_{(y)}} + \Delta_{yaw} \\ 0, & \text{otherwise.} \end{cases}$$
(13)

The PDF for the azimuth displacement $f_{\theta}(\Delta_{\theta})$ is calculated in Eq.(14) by normalizing $f_{\theta_{\mathcal{U}}}(\Delta_{\theta})$, and represents the probability for $\Delta_{\theta} = \Delta_{\theta_{(y)}} + \Delta_{yaw}, \forall \Delta_{\theta_{(y)}}, \Delta_{yaw} \in [-\pi, \pi]$, in order to account for possible compensation in θ .

$$f_{\theta}(\Delta_{\theta}) = \frac{f_{\theta_{\mathcal{U}}}(\Delta_{\theta})}{\int\limits_{-\pi}^{\pi} f_{\theta_{\mathcal{U}}}(\Delta_{\theta}) d_{\Delta_{\theta}}}$$
(14)

The PDF for the displacement in the elevation dimension $f_{\varphi}(\Delta_{\varphi})$, is likewise obtained from Eqs.(12-14), by replacing Δ_{yaw} by Δ_{pitch} and $\Delta_{\theta_{(y)}}$ by the projection over φ of the translational displacement along z-axis $\Delta_{\varphi_{(x)}}$, as per Eq.(10).

4.2.4 Modelling Fading for Sub-Optimal Beam Selection

In Fig. 7a, we showed that the motion experienced by hovering UAVs may cause the selection of sub-optimal pair of beams when beam-sweeping procedure completes. Further, in Fig. 5b, we illustrated how the selection of a certain pair of beams determines (i) the loss at the center of the hovering displacement range $L_{SubOpt}|_{(u,v)}$, as the addition of L_{Tx} and L_{Rx} , and (ii) the range of values of the antenna gain utilized for transmission and reception as the UAV hovers during the complete flight time. For these reasons, given the high dependence of fading on the particular pair of beam selected, the next step towards building our proposed channel model is to determine the set of candidate pair of beams in azimuth and elevation dimensions to which transmitter and receiver may point, post beam-sweeping. To do so, we do not assume that $\{\theta_T, \varphi_T\}$ for transmitter and $\{\theta_R, \varphi_R\}$ for receiver are independent from each other. Instead, we consider that for a particular beam $\{\theta_T, \varphi_T\}$, only a subset of all possible $\{\theta_R, \varphi_R\}$ can achieve alignment between transmitter and receiver, which also depends on UAV hovering motion. Thus, we determine the subset of all possible combinations of $\{(\theta_T, \theta_R), (\varphi_T, \varphi_R)\}$ which are candidate pair of beams.

Moreover, as illustrated in Fig. 2, alignment and thus, beam selection occurs when both transmitter and receiver point to the same angular direction, e.g., both to the same $+\theta$ for the azimuth dimension, as they are located facing each other. Thus, we define the subset of candidate pair of beams indexes as $S = \{u, v\}$, associated to $\{\theta_u, \varphi_v\}$ equal for transmitter and receiver, with $u \in \{1, ..., U\}, v \in \{1, ..., V\}$, where U, V are the number of candidate angular directions in θ and φ dimensions respectively, and $N_b = U \cdot V$, the total number of candidate pair of beams evaluated. The set of possible candidates S depends on (i) the beamforming training parameters, (Section 4.2.1) and shown in Fig. 7b, and (ii) the hovering conditions and the distance between transmitter and receiver, jointly characterized through $f_{\theta}(\Delta_{\theta}), f_{\varphi}(\Delta_{\varphi})$ (Section 4.2.3). Thus, given the stochastic nature of hovering, we need to determine the probability for each candidate pair of beams $(u, v) \in S$ to be selected, in order to provide an accurate loss estimation.

To this extent, we first determine the PDF for the ground receiver node to direct its beam toward a certain angular direction $f_R(\theta)$. For a static case, this term only depends on the angular distribution determined by the beamforming training parameters $f_{R_{SW}}(\Delta_{\theta_{SW}}, \delta_{\theta_{SW}})$, and is given by:

$$f_{R}(\theta) = f_{R_{SW}}(\Delta_{\theta_{SW}}, \delta_{\theta_{SW}}) = \begin{cases} \frac{1}{U}, & \text{if } \theta = p \cdot \delta_{\theta_{SW}}, \forall \theta \in \Delta_{\theta_{SW}} \\ 0, & \text{otherwise.} \end{cases}$$
(15)

With $p \in \mathbb{Z}$. We similarly determine $f_R(\varphi)$ in the elevation dimension considering $\Delta_{\varphi_{SW}}$, $\delta_{\varphi_{SW}}$ and replacing U by V. Moreover, the probability for the UAV transmitter node to direct its beam toward a certain angle $f_T(\theta)$ is jointly determined by the distribution given the beamforming training parameters at the transmitter side $f_{T_{SW}}(\Delta_{\theta_{SW}}, \delta_{\theta_{SW}})$ and the UAV hovering distribution $f_{\theta}(\Delta_{\theta})$. We formally define its unnormalized distribution as:

$$f_{T_{\mathcal{U}}}(\theta) = \int_{-\pi}^{\pi} \int_{-\pi}^{\pi} f_{T_{SW}}(\theta_{SW}) f_{\theta}(\Delta_{\theta})$$

$$\delta(\theta - \theta_{SW} - \Delta_{\theta}) d_{\Delta_{\theta}} d_{\theta_{SW}}$$
(16)

Where δ was defined in Eq.(13), and the normalized version of Eq.(16), $f_T(\theta)$, is obtained similar to Eq.(14). We could further generalize this analysis by considering transmitter and receiver beamforming training parameters to be different from each other, by simply using different $\Delta_{\theta_{SW}}$, $\delta_{\theta_{SW}}$ values in Eqs.(15) and (16). Next, we estimate the probability for a given pair of sub-optimal beams to be selected after beam-sweeping from the following PDF:

$$f_{SubOpt}(\theta,\varphi) = \frac{f_T(\theta)f_R(\theta)f_T(\varphi)f_R(\varphi)}{\int\limits_{-\pi}^{\pi}\int\limits_{-\pi}^{\pi}f_T(\theta)f_R(\theta)f_T(\varphi)f_R(\varphi)d_\varphi d_\theta}$$
(17)

Where the aforementioned dependency between candidate beams has been included, only considering those candidate beams that meet $\theta = \theta_{Tx} = \theta_{Rx}$. Then, the probability for a certain pair of beams (u,v) to be selected after beamsweeping is given by:

$$P(u,v) = \int_{\theta_u - \theta_\Gamma}^{\theta_u + \theta_\Gamma} \int_{\varphi_v - \varphi_\Gamma}^{\varphi_v + \varphi_\Gamma} f_{\mathcal{S}ubOpt}(\theta,\varphi) d_{\varphi} d_{\theta}$$
(18)

Where $\theta_{\Gamma} = \frac{\theta_{u+1} - \theta_u}{2}$, $\varphi_{\Gamma} = \frac{\varphi_{v+1} - \varphi_v}{2}$. Moreover, we formulate the fading caused by the selection of a sub-optimal pair of beams (u,v) according to Fig. 5b, as:

$$L_{SubOpt}|_{(u,v)} = L_{Tx}(\theta_u) + L_{Rx}(\theta_u) + L_{Tx}(\varphi_v) + L_{Rx}(\varphi_v)$$
(19)

Where each fading term is directly obtained from the 3-D aerial h_a and static h_s radiation patterns. To illustrate this process, we set forth the following example. First, the fading term at the transmitter side for the candidate beam u in the azimuth dimension, denoted as $L_{Tx}(\theta_u)$, is calculated as the difference between the transmitter (aerial) antenna radiation pattern h_a evaluated at θ_u , and the radiation pattern maximum value. Notice that the radiation pattern maximum values in θ and φ dimensions correspond to the antenna broadside directions θ_{bs} , φ_{bs} , i.e., the maximum of the radiation pattern, normal to the axis of the array, as we

show in Fig. 5b. Following this, we estimate the fading terms in Eq.(19) as:

$$L_{Tx}(\theta_u) = h_a(\theta_{bs}) - h_a(\theta_u)$$
(20a)

$$L_{Rx}(\theta_u) = h_s(\theta_{bs}) - h_s(\theta_u)$$
(20b)

$$L_{Tx}(\varphi_v) = h_a(\varphi_{bs}) - h_a(\varphi_v)$$
(20c)

$$L_{Rx}(\varphi_v) = h_s(\varphi_{bs}) - h_s(\varphi_v)$$
(20d)

With the formulation provided in this section, we are now able to estimate the fading caused by a sub-optimal beam selection L_{SubOpt} , for a given pair of beams (u,v) within the 3-D space, which is selected with a probability dictated by $f_{SubOpt}(\theta, \varphi)$.

4.2.5 Modelling Fading for Beam Misalignment

In order to provide a stochastic total link fading estimation, we recall to Section 4.2.2. In particular, in Eq.(3), we justified that, estimating the probability for the link to experience a total fading given the selection of a pair of beams after beam-sweeping $P(L_{Tot}|_{(u,v)})$, is reduced to estimating the probability of the sum between misalignment loss and translational displacement along the radial dimension $P(L_{\Delta r} + L_{Misal}|_{(u,v)})$, by exploiting the deterministic nature of every other fading term involved. Thus, in order to estimate $P(L_{Tot}|_{(u,v)})$, we first define the joint distribution for beam misalignment as:

$$f_{Misal}(\Delta_{\theta}, \Delta_{\varphi}) = f_{\Delta_{\theta}}(\Delta_{\theta}) f_{\Delta_{\varphi}}(\Delta_{\varphi})$$
(21)

Where $f_{\Delta_{\theta}}(\Delta_{\theta})$, $f_{\Delta_{\varphi}}(\Delta_{\varphi})$ are the PDFs for the UAV hovering displacement in azimuth and elevation characterized in Section 4.2.3, assumed to be independent from each other. The probability for a given misalignment loss $P(L_{Misal}|_{(u,v)})$ can be directly obtained by integrating Eq.(21). Then, we estimate the probability for a certain $L_{Tot}|_{(u,v)}$ as:

$$P(L_{Tot}|_{(u,v)}) = \iiint_{\Omega_{(\Delta_r,\Delta_\theta,\Delta_\varphi)}} f_{Misal}(\Delta_\theta, \Delta_\varphi) f_r(\Delta_r) d_{\Delta_r} d_{\Delta_\varphi} d_{\Delta_\theta}$$
(22)

With:

$$\Delta_r \in [-\infty, \infty], \quad \Delta_{\theta}, \Delta_{\varphi} \in [-\pi, \pi], \quad \Omega_{(\Delta_r, \Delta_{\theta}, \Delta_{\varphi})} \subset C$$

Where *C* is the set containing all possible combinations of UAV displacements in the radial, azimuth and elevation dimensions $\{(\Delta_r, \Delta_\theta, \Delta_\varphi)\}$ and Ω is the subset of *C* such that the loss term $L_{\Delta_r} + L_{Misal}|_{(u,v)}$ for the subset of displacements considered meets Eq.(4) for a given $L_{Tot}|_{(u,v)}$ value. The loss term L_{Δ_r} is due to small variations on the distance between transmitter and receiver as the UAV hovers, causing path loss fluctuations given by:

$$L_{\Delta_r}(dB) = 10 \cdot \log(\frac{d + \Delta_r}{d})^2$$
(23)

Moreover, misalignment loss is caused by displacements in the θ and φ dimensions given a particular pair of beams $L_{Misal}|_{(u,v)}$, and is directly obtained from the static and aerial 3-D antenna radiation patterns. The calculation is similar to Eqs.(20a-20d), with the particularity that misalignment loss is not calculated as additional loss compared to the broadside direction θ_{bs} , but instead, compared to the angular direction for the specific pair of beams selected (θ_u, φ_v) :

$$L_{Tx}(\Delta_{\theta}) = h_{a}(\theta_{u}) - h_{a}(\theta_{u} + \Delta_{\theta})$$
(24a)
$$L_{Tx}(\Delta_{x}) = h_{a}(\theta_{u}) - h_{a}(\theta_{u} + \Delta_{x})$$
(24b)

$$L_{Rx}(\Delta_{\theta}) = h_{s}(\theta_{u}) - h_{s}(\theta_{u} + \Delta_{\theta})$$
(24b)

$$L_{Tx}(\Delta_{\varphi}) = h_a(\varphi_v) - h_a(\varphi_v + \Delta_{\varphi})$$
(24c)

$$L_{Rx}(\Delta_{\varphi}) = h_s(\varphi_v) - h_s(\varphi_v + \Delta_{\varphi})$$
(24d)

We then have:

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$$L_{\Delta_{\theta}}|_{(u,v)} = L_{Tx}(\Delta_{\theta}) + L_{Rx}(\Delta_{\theta})$$
(25)

$$L_{\Delta_{\varphi}}|_{(u,v)} = L_{Tx}(\Delta_{\varphi}) + L_{Rx}(\Delta_{\varphi})$$
(26)

Which together determine the 3-D misalignment loss:

$$L_{Misal}|_{(u,v)} = L_{\Delta_{\theta}}|_{(u,v)} + L_{\Delta_{\varphi}}|_{(u,v)}$$
(27)

Notice that in contrast to Eqs.(20a-20d), where (θ_u, φ_v) remained constant for a particular pair of beams, here $(\Delta_{\theta}, \Delta_{\varphi})$ vary over time as the UAV hovers. Then, the probability for $L_{Misal}|_{(u,v)}$ to be below a certain threshold γ_{th} is defined as:

$$P(L_{Misal}|_{(u,v)} \le \gamma_{th}) = \iint_{\Omega_{(\Delta_{\theta}, \Delta_{\varphi})}} f_{Misal}(\Delta_{\theta}, \Delta_{\varphi}) d_{\Delta_{\varphi}} d_{\Delta_{\theta}}$$
(28)

With:

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$$\mathbf{Q}_{(\Delta_{\theta}, \Delta_{\varphi})} = \{ (\Delta_{\theta}, \Delta_{\varphi}) \} / L_{\Delta_{\theta}}|_{(u, v)} + L_{\Delta_{\varphi}}|_{(u, v)} \le \gamma_{th}$$

And $P(L_{Tot}|_{(u,v)} \le \gamma_{th})$ can be similarly obtained from Eq.(22) considering $P(L_{\Delta_r} + L_{Misal}|_{(u,v)}) \le \gamma_{th})$.

Additionally, we estimate the average total link fading $\overline{L_{Tot}}$ and average hovering fading $\overline{L_{Hov}}$ given in Eqs.(7) and (6) from (i) the probability for a certain pair of beams to be selected after beam-sweeping, P(u, v), given in Eq.(18), (ii) the fading caused by a sub-optimal beam selection, $L_{SubOpt}|_{(u,v)}$, given in Eq.(19), and (iii) the averaged beam misalignment fading $\overline{L_{Misal}}|_{(u,v)}$ and the average loss caused by translational displacement along the radial dimension $\overline{L_{\Delta_r}}$ given by:

$$\overline{L_{Misal}}|_{(u,v)} = \sum_{\Delta_{\theta}, \Delta_{\varphi}} (L_{\Delta_{\theta}}|_{(u,v)} + L_{\Delta_{\varphi}}|_{(u,v)}) \cdot P(\Delta_{\theta})P(\Delta_{\varphi}))$$
(29)
$$\overline{L_{\Delta_{r}}} = \sum_{\Delta_{r}} L_{\Delta_{r}} \cdot P(\Delta_{r})$$
(30)

Where $P(\Delta_r), P(\Delta_{\theta})P(\Delta_{\varphi})$ can be obtained by directly integrating the PDFs derived in Section 4.2.3, and $\sum_{\Delta_{\theta}, \Delta_{\varphi}} (P(\Delta_{\theta})P(\Delta_{\varphi})) = \sum_{\Delta_r} P(\Delta_r) = 1.$

Finally, for completeness, we define $\overline{L_{\Delta_{\theta}}}$ and $\overline{L_{\Delta_{\varphi}}}$ as:

$$\overline{L_{\Delta_{\theta}}}|_{(u,v)} = \sum_{\Delta_{\theta}} L_{\Delta_{\theta}}|_{(u,v)} \cdot P(\Delta_{\theta})$$
(31)

$$\overline{L_{\Delta_{\varphi}}}|_{(u,v)} = \sum_{\Delta_{\varphi}} L_{\Delta_{\varphi}}|_{(u,v)} \cdot P(\Delta_{\varphi})$$
(32)

Fig. 10 illustrate a channel model flow diagram which all inputs and dependencies considered. The model proposed here is leveraged in Section 5, where we present an algorithm to diminish hovering-related loss caused by a sub-optimal beam selection. Specifically, we apply this model in the upcoming Eqs. (36)- (38), in order to estimate the link loss in all three dimensions θ , φ and r.



Fig. 10: Channel model flow diagram

5 ALGORITHM FOR BEAM OPTIMIZATION IN UAVS

In Figs. 7a and 7c we experimentally demonstrated the large additional fading compared to static scenarios that the selection of a sub-optimal pair of beam introduces, highly degrading the SNR at the receiver. Motivated by this, we next develop an algorithm to find a near-to-optimum pair of beams, alternative to the standard, with the goal of enhancing the average SNR at the receiver, and thus, the mmWave communication link performance.

5.1 Algorithm Intuition

A major cause for link performance degradation is the selection of a pair of beams whose performance is evaluated when the UAV location is close to the boundaries of its hovering displacement range (*Location 1* in Fig. 2). Thus, even though the selected pair of beams achieves the highest performance over all candidate pairs at that location, the tendency of the UAV to move back to the most likely hovering region (*Location 2* in Fig. 2), results in strong beam misalignment in average, for the selected pair of beams.

Our proposed algorithm prevents this situation by allocating weights to the measured received power, for every candidate pair considered during beam-sweeping. The weights $w \in [0, 1]$ are given according to the particular UAV location within the hovering range in which each pair of beams performance is determined. This is, pair of beams evaluated at different locations have distinct *w* values. With this approach, we aim to quantify trough *w* the likelihood that a hovering UAV stays at the location in which the performance of each pair of beams is measured, being w = 1the highest. Thus, taking the example in Fig. 2, w values tend to 1 for those pairs evaluated close to *Location 1*, and tend to 0 for those pairs evaluated in the surroundings of Location 2. Notice that *w* serves as a stochastic confidence metric of the frequency for transmitter and receiver to be aligned over time, and thus, to provide their maximum antenna gains. Given *w* dependency on the UAV location, its value is conditioned by the hovering statistics, and in particular, by the angular and radial displacements $\{\Delta_r, \Delta_\theta, \Delta_\varphi\}$ already characterized in Section 4.2.3.

5.2 Relative Time Scales Magnitude

In this section, we introduce the concept of temporal scale, in order to provide an algorithmic solution applicable to diverse types of systems. We start by defining the time scale magnitude as the complete time-span the sounders take to perform beam-sweeping and evaluate the link performance for all pair of beams. In the WiFi standard 802.11ad, this process takes up to 30 ms, being lower in the 802.11ay release [45]. During such time, the UAV transmitter change of location is negligible, given the long time-span effect of hovering. We denote this condition as Small Temporal Scale (STS). Notice that under STS conditions, w value remains the same for every pair of beams, as they are all evaluated at the same UAV location. We however, chose to extend the algorithm evaluation to a generic case, in which the transmitter location may randomly vary during the beam-sweeping time, and within the hovering maximum displacement range. We denote this condition as Large Temporal Scale (LTS). To evaluate our work performance under LTS conditions, we operate beam-sweeping within a time-span of 2 minutes. During this time, different subsets of beams within the angular beam-sweeping range $\Delta \theta_{SW}$ are evaluated every few seconds.

Notice that LTS is a generalized case of STS conditions, where the UAV location changes over time, and thus, different pair of beams have different *w* values. Thus, we focus on LTS scenarios, and demonstrate that, even under the most generic conditions, our algorithm is still capable of determining a near-to-optimum pair of beams.

5.3 Formulating Confidence-Cost Weights

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Given the *w* dependence on the UAV hovering displacements, discussed in Section 5.1, we formulate *w* as a function of the PDF in the radial dimension calculated from Eqs.(8) and (11), as well as the PDFs in the azimuth and elevation dimensions obtained from Eqs. (12)- (14), as follows:

$$w_k(\Delta_r) = \frac{f_r(\Delta_{r_k})}{f_r(\Delta_r = \mu_{\Delta_r})}$$
(33)

$$v_k(\Delta_\theta) = \frac{f_\theta(\Delta_{\theta_k})}{f_\theta(\Delta_\theta = \mu_{\Delta_\theta})}$$
(34)

$$w_k(\Delta_{\varphi}) = \frac{f_{\varphi}(\Delta_{\varphi_k})}{f_{\varphi}(\Delta_{\varphi} = \mu_{\Delta_{\varphi}})}$$
(35)

With $k \in \{1, ..., N_b\}$ and N_b the total number of pair of beams evaluated. According to this definition, let us consider a pair of beams k that was evaluated during beamsweeping close to the center of the hovering displacement range in r and θ dimensions, $\Delta_{rk} \approx \mu_{\Delta_r}, \Delta_{\theta k} \approx \mu_{\Delta_{\theta}}$, but close to the boundaries of the hovering displacement range in φ dimension $\Delta_{\varphi_k} \approx \mu_{\Delta_{\varphi}} + 3\sigma_{\Delta_{\varphi}}^2$. Then, w_k values according to Eqs. (33)-(35) are $w_k(\Delta_r), w_k(\Delta_{\theta}) \approx 1$ and $w_k(\Delta_{\theta}) \approx 0$, showing high *confidence* for the UAV to remain at the radial and azimuth locations in which the pair of beams k was evaluated during beam-sweeping, and low *confidence* to remain at its elevation location.

Notice that the previous formulation gives the same relevance to *w* in all three dimensions (r, θ, φ) However, not all types of displacements in (r, θ, φ) cause the same degree of



Fig. 11: Empirical validation of existing and proposed channel models. Experimental data collected over 10 minutes is compared with (a) the FSPL and Ideal-Hovering models, (b) the Aerial-Hovering model and (c) the Proposed model

fading. Specifically, in Section 3.3, we experimentally proved that displacements in θ and φ dimensions cause fading of up to 30 dB due to a sub-optimal beam selection as well as beam misalignment, highly related to the 3-D antenna radiation patterns. On the contrary, displacements along the radial dimension only cause fading fluctuations lower than 1 dB for the typical hovering conditions we specified in Section 4.2.3. Therefore, we adjust w_k according to the averaged fading expected in each dimension as follows:

$$w_{L_k}(\Delta_r) = w_k(\Delta_r) \cdot (1 - \frac{L_{\Delta_r k}}{L_{hov_k}})$$
(36)

$$w_{L_k}(\Delta_{\varphi}) = w_k(\Delta_{\theta}) \cdot (1 - \frac{\overline{L_{\Delta_{\theta}k}}}{\overline{L_{hov_k}}})$$
(37)

$$w_{L_k}(\Delta_{\varphi}) = w_k(\Delta_{\varphi}) \cdot (1 - \frac{\overline{L_{\Delta_{\varphi}k}}}{\overline{L_{hov_k}}})$$
(38)

Where $\overline{L_{hov_k}} = \overline{L_{\Delta_r k}} + \overline{L_{\Delta_{\varphi} k}} + \overline{L_{\Delta_{\varphi} k}}$, and these last three terms are derived in Eqs.(30)-(32). By doing so, the weights w_{L_k} , include a stochastically determined *cost* related to the probability for the UAV to suffer from fading in each dimension, if the pair of beams k is selected. This *cost*, together with degree of *confidence*, jointly determine the near-to-optimum pair of beams k^* , ensuring high average performance.

5.4 Algorithm Formulation and Execution

Algorithm 1 presents the execution flow of our proposed method in an actual experiment. The algorithm requires as inputs the received power from the mmWave sounder units, as well as UAV localization data. During the standard beam-sweeping, the sounder units generate time-stamped (*ts*) power measurements for each of the N_b pair of beams evaluated (Algorithm 1, input 1), which are forwarded to the central computer through a control channel by an Ethenet link. In addition, the RTK-GPS EMLID Reach M+ stores the time-stamped *M* coordinate samples collected for the complete beam-sweeping time t_{Sweep} , as the UAV hovers (input

Algorithm 1 Near-to-optimum beam selection under hovering conditions

Input: $(pow)_{k \leftarrow ts}, k = 1...N_b, N_b$ pairs evaluated **Input:** $(x, y, z)_{m \leftarrow ts} \leftarrow (lat, long, alt)_{m \leftarrow ts}, m = 1...M,$ *M* GPS-RTK measurements collected during t_{Sweep} **Output:** k^* , $k \in [1...N_b]$ **1.** Build ts-mapping matrix $M \in \mathbb{R}^{2 \times N_b}$ $H = [(pow)_{k \leftarrow ts}; (x, y, z)_{k \leftarrow ts}]$ **2.** Compute hovering statistics from $(x, y, z)_m \forall m$ $f_r(\Delta_r) \approx f(x - \mu_x)$ $(-\mu_y))$ $f_{\theta}(\Delta_{\theta}) \approx f(atan(\frac{\gamma}{2}))$ $f_{\varphi}(\Delta_{\varphi}) \approx f(atan(\underline{z-\mu_z}))$ $f_{\varphi}(\Delta_{\varphi}) \approx f(atan(\underline{z-\mu_z}))$ **3.** Compute expected losses $\overline{L_{\Delta_r k}}, \overline{L_{\Delta_{\theta} k}}, \overline{L_{\Delta_{\phi} k}}$ as in Eqs.(30)-(32)**4.** Compute weights $w_k(\Delta_r), w_k(\Delta_\theta), w_k(\Delta_\varphi)$ from Eqs. (33)-(35)**5.** Adjust weights $w_{L_k}(\Delta_r), w_{L_k}(\Delta_\theta), w_{L_k}(\Delta_\varphi)$ from Eqs. (36)-(38)6. Find: $k^* = max_k \{pow_k w_{L_k}(\Delta_r) + pow_k w_{L_k}(\Delta_\theta) + pow_k w_{L_k}(\Delta_\varphi)\}$

2). Once beam-sweeping is completed, we access localization data from the host computer through a WiFi link and convert it from geographic (latitude, longitude, altitude) to UTM (Universal Transverse Mercator) coordinates (x, y, z). Then, through the time-stamps, we associate the power measurement for each pair of beams pow_k with the UAV coordinates at the evaluation instant, generating a resultant mapping matrix H (step 1). From the UAV coordinates data collected over t_{Sweep} , we build the UAV hovering statistics (step 2). We use these, together with the static and aerial antenna radiation patterns, to find the estimated losses for each dimension r, θ , φ (step 3), and eventually, the weights for each pair of beams w_k (steps 4, 5). We apply the resultant weights to the measured power for each pair pow_k (step 6), and select the near-to-optimum pair of beams as:

$$k^* = max_k \{pow_k w_{L_k}(\Delta_r) + pow_k w_{L_k}(\Delta_\theta) + pow_k w_{L_k}(\Delta_\varphi)\}$$
(39)

indele 4. novering parameters for fig. 12a			
Maximum			
displacement	$\sigma_{\Delta_x}^2$	$\sigma^2_{\Delta_{\theta_{\mathcal{V}}}} _{d=6m}$	$\sigma_{\Delta_{\theta_{\mathcal{N}}}}^2 _{d=20m}$
$\approx 3\sigma_{\Delta_x} = 3\sigma_{\Delta_y}$		0 y	U, U
0.1 m	$1.09 \cdot 10^{-3}$	$3.08 \cdot 10^{-5}$	$2.78 \cdot 10^{-6}$
0.2 m	$4.36 \cdot 10^{-3}$	$1.23 \cdot 10^{-4}$	$1.11 \cdot 10^{-5}$
0.4 m	0.0177	$4.84 \cdot 10^{-4}$	$4.44 \cdot 10^{-5}$
0.6 m	0.04	$1.09 \cdot 10^{-3}$	$9.99 \cdot 10^{-5}$
0.8 m	0.07	$1.93 \cdot 10^{-3}$	$1.77 \cdot 10^{-4}$
1 m	0.11	$3.03 \cdot 10^{-3}$	$2.77 \cdot 10^{-4}$
1.5 m	0.25	$8.31 \cdot 10^{-2}$	$2.5 \cdot 10^{-2}$
0.8 0.6 0.4 0.2	0.1 m 0.1 m 0.4 m 0.6 m 0.6 m 0.8 m 0.8 m 0.4 0.8 m 0.4		

TABLE 4: Hovering parameters for Fig. 12a



—6 m

120

110

Path Loss (dB)

(b)

100

••• 1.5 m

130

100

110 120

(a)

Path Loss (dB)

Note that k^* is optimal only in a static case, where there is no UAV hovering-related motion. With hovering and STS conditions, w_{L_k} values are equal for all N_b pair of beams in each dimension, and k^* is selected only based on pow_k , same as the standard. However, notice that if the one location where all N_b pairs are evaluated differs from the center of the UAV hovering displacement distribution in any of the three dimensions, k^* is still sub-optimal in average under STS conditions. In this case, a better pair can be chosen by exploiting the hovering stochastic distributions provided by our model. In a more general case, under LTS conditions, in which each pair of beams is evaluated at different locations, finding the optimum pair is not always feasible, since there is no guarantee that perfect alignment occurs within t_{Sweep} . In this case, k^* given by Eq.(39) is a near-to-optimum solution, i.e., the best possible solution given the available data.

6 EXPERIMENTAL RESULTS

We first provide experimental validation for the analytical channel model formulated in Section 4, using data collected during UAV actual flights, in Section 6.1. In this section, we also provide simulation results for multiple scenarios using the model. Then, in Section 6.2, we experimentally demonstrate the performance gain achieved with the proposed beam selection algorithm presented in Section 5.

Our setup here is similar to the description provided in Section 3.3.2 and illustrated in Fig6, consisting of a TG sounder unit mounted on a M600 DJI UAV, acting as transmitter, and a second unit as static ground receiver. Only for the results presented in Fig. 15, the transmitter is mounted on a mobile slider in order to emulate the UAV hovering motion without battery constraints. All other results were obtained under actual flight.

6.1 Channel Model Validation

In order to validate the fading estimation provided by our channel model, we establish a UAV-to-Ground link with the

setup in Fig. 6. Once the UAV is hovering during actual flight, we perform beam-sweeping and fix the best pair of beams for transmission, according to the standard. We maintain the selected pair over the remaining UAV flight time (\approx 10 minutes). From the experimental data collected, we build the Cumulative Distribution Function (CDF) of the UAV-to-Ground link path loss, in Fig. 11. The error deviation of the experimental data is a hardware-specific feature, with a value of up to 4 dB. Alongside with it, we provide the estimated path loss using different analytical channel models. In particular, in Fig. 11a we consider (i) the FSPL model, which only accounts for frequency and distance between transmitter and receiver and (ii) the Misalignment Loss, Ideal Beampattern model, in which we include the ideal antenna radiation pattern with a beamwidth of 2.8°, shown in Fig. 4, as well as power fluctuations caused by beam misalignment, estimated through real hovering data collected over time during the experiment. The latter model comes closest to existing works in the literature [31], in which the authors only account for misalignment loss and the main lobe of an ideal antenna radiation pattern, neglecting the effect of secondary side lobes.

In addition, in Fig. 11b we present the estimated path loss using (iii) the Misalignment Loss, Aerial Beampattern model, in which we replace the ideal radiation pattern in the previous model by the 3-D aerial radiation pattern in Fig. 14b, built from the aerial 2-D azimuth slice in Fig. 4, and a 2-D elevation slice with $\theta_{3dB} = 50^{\circ}$ built in simulation using antenna array synthesis. Thus, in this model, we account for L_{Afr} , additional losses caused by the UAV airframe. We include theoretical bounds for the analytical models, estimated by considering an error of 20% on the typical deviation for the hovering statistical distributions. This provides a fair comparison between models if insufficient hovering data is collected, given the UAV battery constraints, or under the presence of anomalies during data collection. Lastly, in Fig. 11c, we present the path loss estimation given by (iv), our Proposed Model. This, in addition to misalignment loss and realistic 3-D aerial and static radiation patterns, includes the effect of sub-optimal beam selection after beam-sweeping. Specifically, we include the estimated loss for each candidate pair of beams (dashed blue lines), stochastically determined by a Monte Carlo simulation, as well as their averaged value. Notice that our Proposed Model provides the closest estimation to the experimentally measured path loss, which is seen as a particular realization of the probabilistic estimation we provide. Moreover, the results presented here clearly reveal the accuracy gain achieved when the effect of each UAVrelated fading component discussed so far, is added to the model. In particular, our model drops estimation error to \approx 0.2%, approximately 18x lower than the *Misalignment* Loss, Ideal Beampattern model, the closest to the state-ofthe-art models existing in the literature. Next, we use our UAV-to-Ground channel model in order to estimate the total fading L_{Tot} in a 60 GHz link for multiple scenarios. In Fig. 12a, we present simulation results for the CDF of the total path loss, tailored to different maximum UAV hovering displacements, considered to be equal in θ and φ dimensions. For all cases in Fig. 12a, we set the distance between transmitter and receiver to d = 6 m. In Table 4, we



Fig. 13: Total fading for different (a) beam-sweeping angular range and hovering conditions, (b) beam-sweeping angular resolution and hovering conditions and (c) 3-D radiation patterns



Fig. 14: 3-D normalized radiation patterns with $\{\theta_{3dB}, \varphi_{3dB}\}$: (a) $\{2.8^{\circ}, 2.8^{\circ}\}$, (b) $\{2.8^{\circ}, 50^{\circ}\}$, (c) $\{2.8^{\circ}, 8.5^{\circ}\}$ and (d) $\{5^{\circ}, 5^{\circ}\}$

provide the UAV hovering statistics used for this simulation. In addition, we include the hovering statistics for a case of d = 20m. In Fig. 12b we estimate the total link path loss for different d values. We observe how additional link fading is encountered as UAV hovering displacement grows and distance shrinks.

In Figs. 13a and 13b, we present simulation results for different beamforming training parameters and two different UAV hovering displacements, 0.6 and 1.5 m, respectively representing typical and strong hovering conditions. From Fig. 13a, path loss increases as the maximum angular ranges evaluated during beam-sweeping $\Delta \theta_{SW} = \Delta \varphi_{SW}$ grow (max_{SW} in the figure). This is expected, since for large $\Delta \theta_{SW}, \Delta \varphi_{SW}$ values, the selected pair of beams can potentially be further from the antenna main lobe (broadside direction). Moreover, as maximum hovering displacement (max_{hov} in the figure) becomes more severe, chances for suboptimal beam selection increase, leading to a worst average link performance. In addition, from Fig. 13b, we observe that path loss decreases with the angular beamforming resolution δ_{SW} .

In Fig. 14 we present different 3-D radiation patterns created from real measurements in an anechoic chamber (cases of 2.8° and 8.5°) and simulation (all other beamwidths). The estimated path loss considering different radiation patterns in presented in Fig. 13c. This results show a tendency for the link to suffer from greater path loss, as beamwidth narrows.

6.2 beam selection Validation

In order to validate our beam selection algorithm, we compare the average performance achieved with our proposed pair of beams and the pair of beams selected by the standard. We remark here that, during actual UAV experiments, we need to evaluate both solutions within a single batterydetermined UAV flight-time (\approx 12 minutes). This prevents



Fig. 15: Initial tests with sounder Tx mounted on slider

vibrations during taking-off and landing from altering relative location between transmitter and receiver and hovering patterns, providing a fair comparison between both solutions. Thus, we perform a two-step validation process, by using two different setups: (i) with the transmitter sounder mounted on a mobile slider that we remotely control in order to emulate the random UAV lateral displacements during hovering without the UAV battery constraint, shown in Fig. 15 and (ii), during actual UAV flights with the setup shown in Fig. 6. For both setups, once the UAV is in hovering motion, we perform beam-sweeping followed by beam selection according to the 802.11ad standard. We maintain the selected pair of beams for half the UAV flighttime. We then find a near-to-optimum pair of beams according to Algorithm.1, and fix it for the second half of the UAV flight-time. The two inputs required by the algorithm according to Section 5.4 are the measured power obtained from the mmWave sounder units, and the UAV localization data obtained from the low-cost RTK-GPS.

For the first setup, in Fig. 17a we show a comparison between the standard and the proposed solution in terms of the path loss ECDF. Our proposed solution limits the average path loss by 8.7 dB. It does so by selecting a pair of beams evaluated at the center of the UAV hovering displacement range, even though it presented lower performance during the standard-defined beam-sweeping. In Fig. 17b, we present a comparison in terms of PHY bitrate. With our selected pair of beams, the bit-rate is constant at its maximum value, since path loss fluctuations are not sufficient to decrease the modulation order [43], in contrast to the standard-defined solution.

In Figs. 16a- 16c we introduce results for our second



Fig. 16: Experimental results for UAV tests showing a comparison between standard and proposed algorithm in terms of (a) measured path loss during beam-sweeping and selected beams, (b) path loss for selected beams and (c) PHY bit-rate



Fig. 17: Performance comparison between beam selected by standard and proposed algorithm for slider test in terms of (a) path loss and (b) PHY bit-rate

setup, from an actual UAV flight. For this test, we initially locate transmitter and receiver facing each other, and thus, the optimum pair of beams is expected to be close to the antenna broadside directions ($\theta_{bs} = \varphi_{bs} = 0^\circ$) for both sounders. In Fig. 16a, we present the measured path loss for all transmitting and receiving steering angles evaluated during beam-sweeping. Additionally, we highlight the pair of beams selected by the standard and the proposed algorithm. As expected, the standard selects the pair of beams with lowest path loss during evaluation, which is 83.69 dB. However, their angles (-14.1° for transmitter and 5.6° for receiver) are far from the expected broadside angular direction. In contrast, our proposed algorithm selects a different pair of beams in spite of their higher path loss of 99.12 dB during beam-sweeping evaluation, steering toward -2.8 °, both transmitter and receiver. This selection is driven by the trade-off between (i) the higher path loss measured during beam-sweeping, (ii) the more centered UAV location in (r, θ, φ) dimensions within the hovering displacement range, and (iii) the effect the displacement in each dimension has on the expected average total link fading. In Fig. 16b, we compare the path loss experienced using our proposed pair of beams and the one provided by the standard. Our solution achieves an average path loss reduction of 4 dB. In Fig. 16c, we compare the PHY bit-rate for both solutions. In this case, our proposed solution maintains a high bit-rate above 3 Gbps for the 91% of the measurements taken during evaluation, compared to 37% achieved by the standard.

We highlight here that the performance gain achieved with our proposed algorithm varies for each particular realization given its stochastic nature, and it is highly dependent on the hovering pattern, UAV hardware, beam-sweeping training configuration and deployment parameters. From our experimental results, our solution guarantees at least the same performance as the standard, providing a significant average gain when hovering prevents the standard from determining the optimal beam selection.

7 CONCLUSIONS

In this paper, we demonstrate the important issues impacting UAV communications in the 60 GHz mmWave band, in particular those arising from the UAV airframe and the UAV continuous motion during hovering. For the latter, we quantify the effect of beam misalignment and the sub-optimal beam selection encountered when performing conventional beam-sweeping in real UAV scenarios. We build a stochastic analytical channel model to estimate the total path loss in an UAV-to-Ground link, which can be tailored to different UAV hardware, 3-D antenna radiation patterns, beamforming training parameters and deployment conditions. Moreover, driven by the sub-optimal beam selection problem encountered during our experiments, we propose a low-complexity standard-compliant algorithm in order to enhance the average link performance. Overall, we consider that adopting a systems-level approach is the key to provide accurate fading estimations. This includes (i) the effect of the UAV airframe on the antenna radiation pattern, which causes significant fading, (ii) the impact of a sub-optimal beam selection after beam-sweeping, and (iii) power fluctuations caused by beam misalignment, whose magnitude depends on the sub-optimal beam selected as well as on the transmitting and receiving 3-D radiation patterns. We experimentally validate both the channel model and our beam selection algorithm with 802.11ad complaint Terragraph sounder units mounted on DJI M600 UAVs.

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TABLE 5: TABLE OF NOTATIONS

$ \begin{array}{ll} List of Acronyms \\ TG \\ TG \\ TG \\ AWV \\ Antenna Weight Vector \\ RTK \\ Real-Time Kinematic \\ IMU \\ Inertial Measurement Unit \\ EIRP \\ ECDF Empirical Cumulative Distribution Function \\ PHY - bitrate \\ SNR \\ Signal-to-Noise Ratio \\ Tx, Rx \\ Transmitter, Receiver \\ \hline Antenna Parameters \\\hline \theta \\ Azimuth \\ \varphi \\ Elevation \\ \theta_{3dB}, \theta_{3dB} \\ \theta_{3dB}, \theta_{3dB} \\ 3-dB beamwidth in azimuth, elevation \\ \theta_{bs}, \phi_{bs} \\ Broadside direction in azimuth, elevation \\ \theta_{bs}, \phi_{bs} \\ Broadside direction in azimuth, elevation \\ E \\ effective \\ Pd \\ Pd \\ Power density \\ g \\ Antenna gain \\ Pr \\ Received power \\ h_a \\ Arial radiation pattern (UAV) \\ h_s \\ Static radiation pattern (Ground) \\ \hline Beamforming Training Parameters \\ \Delta_{\theta_{SW}}, \Delta_{g_{SW}} \\ Beam-sweeping angular range \\ \delta_{\theta_{SW}}, \delta_{g_{SW}} \\ Beam-sweeping angular resolution \\ UAV toordinate {x, y, z, roll, pitch, yaw} {i \\ i \\ Polar coordinate {x, \theta, Q} } \\ \lambda_{j}, \Lambda_{i} \\ Hovering displacement in coord. j over i \\ \mu_{\Delta_{j}} \\ Mean vale of displacement in j \\ f(\Lambda_{i}) \\ PDF of displacement $	Symbol	Description
$\begin{array}{llllllllllllllllllllllllllllllllllll$	List of Acronyms	
AWVAntenna Weight VectorRT KReal-Time KinematicIMUInertial Measurement UnitEIRPEffective Isotropic Radiated PowerECDFEmpirical Cumulative Distribution FunctionPHY-bitratePhysical layer bitrateSNRSignal-to-Noise RatioTx., RxTransmitter, ReceiverAntenna Parameters θ θ Azimuth φ Elevation $\phi_{odB}, \varphi_{odB}$ 3-dl beamwidth in azimuth, elevation E Electric field Z_0 Free-space impedance P_d Power density g Antenna gain P_r Received power h_a Aerial radiation pattern (UAV) h_s Beam-sweeping angular range $\delta_{gw}, \delta_{gsw}$ Beam-sweeping angular range $\delta_{gw}, \delta_{gsw}$ Beam-sweeping angular range $\delta_{gw}, \delta_{gsw}$ Beam-sweeping angular range $\delta_{fw}, \delta_{gsw}$ Beam-sweeping angular resolutionUAV coordinate {x, y, z, roll, pitch, yaw}iPolar coordinate {x, θ, q $f(\Delta_i)$ PDF of displacement in j $f(\Delta_i)$ PDF of displacement in j $f(\Delta_i)$ Dirac delta function for displacement in i $f(\Delta_i)$ Dirac delta function for displacement in i $f(\Delta_i)$ Distance between transmitter and receiver L_{Afr} UAV airframe-related loss L_{Ar} Distance d fluctuation loss L_{Ar} Distance d functuation loss L_{Tor} Total link loss σ_{r} Re	TG	Terragraph
$ \begin{array}{ll} RK & Real-Ime Kinematic \\ IMU Inertial Measurement Unit \\ EIRP & Effective Isotropic Radiated Power \\ ECDF & Empirical Cumulative Distribution Function \\ PHY - bitrate \\ SNR & Signal-to-Noise Ratio \\ Tx, Rx & Transmitter, Receiver \\ \hline Antenna Parameters \\ \hline \theta & Azimuth \\ \varphi & Elevation \\ \hline \theta_{2d,R}, \varphi_{2d,R} & 3-dB beamwidth in azimuth, elevation \\ \hline \theta_{2d,R}, \varphi_{2d,R} & 3-dB beamwidth in azimuth, elevation \\ \hline \theta_{2d,R}, \varphi_{2d,R} & 3-dB beamwidth in azimuth, elevation \\ \hline E & Electric field \\ Z_0 & Free-space impedance \\ P_d & Power density \\ g & Antenna gain \\ P_r & Received power \\ h_a & Aerial radiation pattern (UAV) \\ h_s & Static radiation pattern (Ground) \\ Beamforming Training Parameters \\ \hline \Delta_{6sw}, \Delta_{\psi_{SW}} & Beam-sweeping angular range \\ \hline \partial_{6sw}, \phi_{\psi_{SW}} & Beam-sweeping angular range \\ \hline \partial_{6sw}, \phi_{\psi_{SW}} & Beam-sweeping angular resolution \\ UAV Hovering Model Parameters \\ \hline i & Polar coordinate {x, y, z, roll, pitch, yaw} \\ i & Polar coordinate {x, y, z, roll, pitch, yaw} \\ i & Polar coordinate {x, y, y, roll, pitch, yaw} \\ \hline \Delta_{f,0} & Mean vale of displacement in j \\ f(\Delta_1) & PDF of displacement in j \\ f(\Delta_1) & DDF of displacement in j \\ f_{G}(\Delta_1) & Distance between transmitter and receiver \\ L_{FSPL} & Free Space Path Loss \\ L_{Afr} & UAV airframe-related loss \\ L_{Mixal} & Beam misalignment loss \\ L_{afr} & Otal link loss \\ \theta_{T, e} & Receiver steering angles \\ \theta_{T, e} & Receiver steering angles \\ \theta_{T, e} & Receiver steering angles \\ \theta_{T, e} & Subsorp & Tatal link loss \\ \theta_{T, o} & Subset of candidate beams (u, v) \\ L_{Tx}(\Delta_{q}) & L_{Tx}(\Delta_{q}) & L_{xist}(\sigma h) overing displacement in i \\ C & Set of all possible combinations of \Delta_i \\ Q & Subset of all possible combinations of \Delta_iQ & Subset of all possible combination i(C & Set of all possib$	AWV	Antenna Weight Vector
$ \begin{array}{rll} DU & Internal Measurement Unit EIRP ElfRP Effective Isotropic Radiated Power ECDF Empirical Cumulative Distribution Function PHY - bitrate Physical layer bitrate SNR Signal-to-Noise Ratio Tx, Rx Transmitter, Receiver Antenna Parameters \theta Azimuth\varphi Elevation\theta_{bsl,B}, \varphi_{3dB} 3-dB beamwidth in azimuth, elevation\theta_{bsl,B}, \varphi_{3dB} 3-dB beamwidth in azimuth, elevation\theta_{bs}, \varphi_{bs} Broadside direction in azimuth, elevationE$ Electric field Zo Free-space impedance P_d Power density g Antenna gain Pr Received power h_a Aeria radiation pattern (UAV) h_s Static radiation pattern (UAV) h_s Static radiation pattern (UAV) h_s Static radiation pattern (UAV) h_s Geaw, φ_{esw} Beam-sweeping angular range $\delta_{dsw}, \delta_{esw}$ Beam-sweeping angular range $\delta_{dsw}, \delta_{esw}$ Beam-sweeping angular resolution UAV toorring Model Parameters J UAV coordinate { $r, y, z, roll, pitch, yaw$ } i Polar coordinate{ r, θ, φ } Δ_{j, Δ_1} Hovering displacement in dimensions i, j $\Delta_{i,j}$, Variance of displacement in j f_{Δ_j} Variance of displacement in j f_{Δ_j} PDF of displacement in j f_{Δ_j} PDF of displacement in j f_{Δ_j} Distance between transmitter and receiver L_{FSPL} Free Space Path Loss L_{Afr} UAV airframe-related loss L_{Afr} Distance d fluctuation loss L_{Afr} Condidate beam sind θ and φ S Suboptin a beam sindegrament in i f_{Sw} Receiver steering angles θ_{R}, φ_{R} Receiver steering angles θ_{R}, φ_{R} Receiver steering angles θ_{R}, φ_{R} Receiver steering angles θ_{R}, φ_{R} Receiver steering angles θ_{R}, ϕ_{R} Receiver steering angles $\theta_{R},$	RTK	Real-Time Kinematic
$\begin{array}{rcl} PAP & \mbox{ECDF} & \mbox{End} Physical layer bitrate BCDF & \mbox{End} Physical layer bitrate SINR & Signal-to-Noise Ratio T x, Rx & Transmitter, Receiver \\ \hline T x, Rx & Transmitter, Receiver \\ \hline Antenna Parameters & \hline \theta & Azimuth \\ \hline \varphi & Elevation \\ \hline \theta_{3dB, \varphi_{3dB} & 3-dB beamwidth in azimuth, elevation \\ \hline \theta_{3dB, \varphi_{3dB} & 3-dB beamwidth in azimuth, elevation \\ \hline \theta_{bs, \varphi_{bs} & Broadside direction in azimuth, elevation \\ \hline B_{bs, \varphi_{bs} & Broadside direction in azimuth, elevation \\ \hline E & Electric field \\ \hline Z_0 & Free-space impedance \\ P_d & Power density \\ g & Antenna gain \\ P_r & Received power \\ h_a & Aerial radiation pattern (UAV) \\ h_s & Static radiation pattern (Ground) \\ \hline Beamforming Training Parameters \\ \hline J & UAV coordinate {x, y, z, roll, pitch, yaw} \\ \hline J & Polar coordinate {x, y, z, roll, pitch, yaw} \\ \hline J & Polar coordinate {x, y, z, roll, pitch, yaw} \\ \hline J & Polar coordinate {x, y, z, roll, pitch, yaw} \\ \hline J & Polar coordinate {x, y, z, roll, pitch, yaw} \\ \hline J & Qay & Ogen \\ \hline Jay & Qay & Qay & Qay \\ \hline J_{i,j} & Projection of displacement in j \\ \hline T & Qay & Qay & Qay \\ \hline J_{i,j} & PDF of displacement in j \\ \hline J_{i,j} & Mean vale of displacement in j \\ \hline J_{i,j} & Qay & Qay & Qay \\ \hline J_{i,k}(A_i) & DTF of displacement in j \\ \hline J_{i,k}(A_i) & DTF of displacement in j \\ \hline J_{i,k}(A_i) & Unnormalized PDF of displacement in i \\ \hline Channel Model Parameters \\ \hline d & Distance between transmitter and receiver \\ L_{FSPL} & Free Space Path Loss \\ L_{A_fr} & UAV aiframe-related loss \\ L_{Mov} & Hovering Pattel doss \\ L_{Mov} & Hovering PIE given beamforming \\ \hline J_{i,k}(A_i) & Distance Brite and receiver \\ L_{fs}(P, f, f(\varphi) & Tx PDF to sweep in certain angle \\ J_{k}(\theta), f_{R}(\varphi) & Xx DPT to sweep in certain angle \\ J_{k}(\varphi), f_{R}(\varphi) & Xx DPT to sweep in certain angle \\ J_{k}(\varphi), f_{k}(\varphi) & Xx DPT for sweep in certain angle \\ J_{k}(A_i), Confidence cost weight, pair k, dimension i \\ C & Set of all possible combination of A_i \\ Q & Subset of C causing a given loss \\ T_{k}(\Delta_i) & Confidence weight, $		Inertial Measurement Unit
$\begin{array}{cccc} Different constraints to Distribution relation relatin relation relation r$		Effective Isotropic Radiated Fower
$ \begin{array}{cccc} SNR & Signal-to-Noise Ratio \\ Tx, Rx & Transmitter, Receiver \\ \hline \\ Antenna Parameters \\ \hline \\ \hline \\ \theta & Azimuth \\ \varphi & Elevation \\ \hline \\ \hline \\ \theta_{3dB}, \varphi_{3dB} & 3-dB beamwidth in azimuth, elevation \\ \hline \\ \hline \\ \theta_{bsdB}, \varphi_{5dB} & 3-dB beamwidth in azimuth, elevation \\ \hline \\ \hline \\ \theta_{bsdB}, \varphi_{5dB} & 3-dB beamwidth in azimuth, elevation \\ \hline \\ \hline \\ \theta_{cs} & Electric field \\ \hline \\ Z_0 & Free-space impedance \\ \hline \\ P_d & Power density \\ g & Antenna gain \\ \hline \\ P_r & Received power \\ h_a & Aerial radiation pattern (UAV) \\ h_s & Static radiation pattern (Ground) \\ \hline \\ Beamforming Training Parameters \\ \hline \\ \hline \\ \Delta_{6wv}, \Delta_{esw} & Beam-sweeping angular range \\ \hline \\ \hline \\ \partial_{6wv}, \delta_{esw} & Beam-sweeping angular resolution \\ \hline \\ UAV Hovering Model Parameters \\ \hline \\ i & UAV coordinate {x, y, z, roll, pitch, yaw} \\ i & Polar coordinate {x, y, z, roll, pitch, yaw} \\ i & Polar coordinate {r, \theta, \varphi} \\ \hline \\ \Delta_{f_1}, A_i & Hovering displacement in dimensions i, j \\ \sigma_{A_1}^{-j} & Variance of displacement in j \\ \sigma_{A_1}^{-j} & Variance of displacement in j \\ \sigma_{A_1}^{-j} & DEF of displacement in j \\ f(\Delta_i) & PDF of displacement in j \\ f_{i}(\Delta_i) & UAV coordinate PDF of displacement in i \\ \delta_{i}(\Delta_i) & UDr of displacement in j \\ f_{i}(\Delta_i) & DDF of displacement in j \\ f_{i}(\Delta_i) & UNnormalized PDF of displacement in i \\ \delta_{A_1} & Dirac delta function for odisplacement in i \\ \delta_{A_1} & Distance between transmitter and receiver \\ EFSPL & Free Space Path Loss \\ L_{Hov} & Hovering -related loss \\ L_{Hov} & Hovering PDF given beamforming \\ L_{A_r} & Distance d fluctuation loss \\ L_{A_r} & Distance d PDF given beamforming \\ f_{R}(\theta), f_{R}(\varphi) & Tx PDF to sweep in certain angle \\ f_{R}(\theta), f_{R}(\varphi) & Tx PDF to sweep in certain angle \\ f_{R}(\theta_r), f_{R}(\varphi) & Tx DDF to sweep in certain angle \\ f_{R}(\theta_r), f_{R}(\varphi) & Tx DDF to sweep in certain angle \\ f_{R}(\theta_r), f_{R}(\varphi) & Tx DDF to sweep in certain angle \\ f_{R}(\theta_r), f_{R}(\varphi) & Tx D$	PHY - hitrate	Physical layer bitrate
A. Transmitter, ReceiverAntenna Parameters θ $Azimuth$ φ Elevation $\theta_{3dB}, \varphi_{3dB}$ 3-dB beamwidth in azimuth, elevation B_{bs}, φ_{bs} Broadside direction in azimuth, elevation E Z_0 $Fee-space impedanceP_dP_dP_dP_eh_aAceial radiation pattern (UAV)h_sh_aAceial radiation pattern (UAV)h_sh_aAerial radiation pattern (Ground)Beamforming Training Parameters\Delta_{6sw}, \Delta_{esw}Beam-sweeping angular resolutionUAV toordinate {x, y, z, roll, pitch, yaw}iDlar coordinate {r, \theta, \varphi}\Delta_{f, 0}A_{f, 0}$	SNR	Signal-to-Noise Ratio
Antenna Parameters θ $Antenna Parameters\theta\varphi\theta_{JdB}, \varphi_{JdB}\beta-dB beamwidth in azimuth, elevation\theta_{bs}, \varphi_{bs}Broadside direction in azimuth, elevation\theta_{bs}, \varphi_{bs}Broadside direction in azimuth, elevation\theta_{cs}P_dP_dP_dP_dP_dP_rReceived powerh_ah_ah_aAerial radiation pattern (Ground)Beamforming Training Parameters\Delta_{\delta gw}, \delta_{\varphi sw}Beam-sweeping angular resolutionUAV Hovering Model ParametersjQ_{bw}, \delta_{\varphi sw}A_{a, A}A_{i, 0}Polar coordinate {x, y, z, roll, pitch, yaw}iPolar coordinate {r, \theta, \varphi}\Delta_{i, j}\Delta_{i, j}Polar coordinate {r, \theta, \varphi\Delta_{i, j}Polar coordinate {r, \theta, \varphi\Delta_{i, j}\Delta_{i, j}Polar coordinate {r, \theta, \varphi\Delta_{i, j}Polar coordinate {r, \theta, \varphi\Delta_{i, j}Polar coordinate {r, \theta, \varphiA_{i, j}A_{i, j}A_{i, j}$	T x R x	Transmitter, Receiver
θAzimuthφElevation $\theta_{\alpha,B}, \varphi_{\alpha,B}$ 3-dB beamwidth in azimuth, elevation $B_{\alpha,S}, \varphi_{\alpha,B}$ Broadside direction in azimuth, elevation E Electric field Z_0 Free-space impedance P_d Power densitygAntenna gain P_r Received power h_a Aerial radiation pattern (UAV) h_s Static radiation pattern (Ground)Beamforming Training Parameters $\Delta_{Bgw}, \Delta_{gew}$ Beam-sweeping angular resolutionUAV Hoeering Model Parameters i UAV coordinate { x, y, z, roll, pitch, yaw} i Polar coordinate { r, θ, φ} $\Delta_{f,0}$ Mean vale of displacement in coord. j over i μ_{Δ_j} Mean vale of displacement in j $f_i(\Delta_i)$ PDF of displacement in j $f_i(\Delta_i)$ PDF of displacement in j $f_i(\Delta_i)$ DDF of displacement in j $f_i(\Delta_i)$ Distance between transmitter and receiver L_{rsPL} Free Space Path Loss L_{A_r} Distance d fluctuation loss L_{Tor} Total link loss θ_r, φ_R Receiver steering angles θ_r, φ_R Receiver steering angles $f_r(0), f_r(\varphi)$ Rx Steering PDF given beamforming f_{asw} Sub-optimal beam selection loss L_{A_r} Distance d fluctuation loss L_{A_r} Distance d fluctuation loss L_{A_r} Distance between transmitter and φ f_{asw} Rx steering PDF given beamforming $f_{R}(\theta), f_R(\varphi)$ <th>Antenna Parameters</th> <th></th>	Antenna Parameters	
$\begin{array}{lll} \varphi & Elevation \\ \theta_{3dB, \varphi_{2dB}} & 3-dB beamwidth in azimuth, elevation \\ \theta_{bs}, \varphi_{bs} & Broadside direction in azimuth, elevation \\ E & Electric field \\ Z_0 & Free-space impedance \\ P_{al} & Power density \\ g & Antenna gain \\ P_r & Received power \\ h_a & Acrial radiation pattern (UAV) \\ h_s & Static radiation pattern (UAV) \\ h_s & Static radiation pattern (Ground) \\ \hline Beamforming Training Parameters \\ \Phi_{gw}, \Delta_{\varphi_{SW}} & Beam-sweeping angular range \\ \Phi_{gw}, \delta_{\varphi_{SW}} & Beam-sweeping angular resolution \\ \hline UAV Hovering Model Parameters \\ \hline J & UAV coordinate \{x, y, z, roll, pitch, yaw\} \\ i & Polar coordinate \{x, y, z, roll, pitch, yaw\} \\ i & Polar coordinate \{x, y, z, roll, pitch, yaw\} \\ i & Polar coordinate of displacement in j \\ \sigma_{A_j}^{-1} & Variance of displacement in j \\ \sigma_{A_j}^{-1} & Variance of displacement in j \\ \sigma_{A_j}^{-1} & Variance of displacement in j \\ f(\Delta_i) & PDF of displacement in j \\ f(\Delta_i) & DDF of displacement in j \\ f_{u}(\Delta_i) & Unnormalized PDF of displacement in i \\ f_{u}(\Delta_i) & Unnormalized PDF of displacement in i \\ Channel Model Parameters \\ d & Distance between transmitter and receiver \\ L_{FSPL} & Free Space Path Loss \\ L_{A_f r} & UAV airfname-related loss \\ L_{A_f r} & UAV airfname-related loss \\ L_{A_f r} & Distance d fluctuation loss \\ L_{A_f r} & Transmitter steering angles \\ \theta_{R}, \varphi_{R} & Receiver steering angles \\ \theta_{R}, \varphi_{R} & Receiver steering angles \\ f_{R}(\theta), f_{R}(\varphi) & Rx PDF to sweep in certain angle \\ f_{r}(\theta), f_{T}(\varphi) & Rx PDF to sweep in certain angle \\ f_{r}(\theta), f_{T}(\varphi) & Tx DDF to sweep in certain angle \\ f_{R}(\phi), f_{R}(\varphi) & L_{SubOp,i}$ at transmitter given pair $(u, v) \\ L_{Tx}(\Delta_{\theta}), L_{Tx}(\Delta_{\varphi}) & L_{SubOp,i}$ at transmitter given pair $(u, v) \\ L_{Tx}(\Delta_{\theta}), L_{Tx}(\Delta_{\varphi}) & L_{SubOp,i}$ at transmitter given pair $(u, v) \\ L_{Tx}(\Delta_{\theta}), L_{Tx}(\Delta_{\varphi}) & L_{SubOp,i}$ at transmitter given pair $(u, v) \\ L_{Tx}(\Delta_{\theta}), L_{Tx}(\Delta_{\varphi}) & L_{SubOp,i}$ at transmitter given pair $(u, v) \\ L_{Tx}(\Delta_{\theta}), L_{Tx}(\Delta_{\varphi}) & L_{SubOp,i}$ at transmitte	θ	Azimuth
$\begin{array}{llllllllllllllllllllllllllllllllllll$	φ	Elevation
$\theta_{hs}, \varphi_{hs}$ Broadside direction in azimuth, elevation E Electric field Z_0 Free-space impedance P_d Power density g Antenna gain P_r Received power h_a Aerial radiation pattern (UAV) h_s Static radiation pattern (Ground)Beamforming Training Parameters $\Delta_{\theta_{SW}}, \Delta_{\varphi_{SW}}$ Beam-sweeping angular range $\delta_{\theta_{SW}}, \delta_{\psi_{SW}}$ Beam-sweeping angular resolutionUAV Hovering Model Parameters j UAV coordinate { $x, y, z, roll, pitch, yaw$ } i Polar coordinate{ r, θ, φ } j_j, Δ_i Hovering displacement in dimensions i, j $A_{i,j}$ Projection of displacement in j $f_{i,j}$ Variance of displacement in j $f_{i,j}$ DF of displacement in j $f_{i,j}(\Delta_i)$ PDF of displacement in i $\delta(\Delta_i)$ Dirac delta function for displacement in i $\delta(\Delta_i)$ Dirac delta function for displacement in i d Distance between transmitter and receiver L_{FSPL} Free Space Path Loss L_{A_f} Distance d fluctuation loss $L_{f,g}(\theta), f_R(\varphi)$ Tx PDF to sweep in certain angle $f_{f,w}$ Total link loss θ_T, φ_R Receiver steering angles θ_{R}, φ_R Receiver steering PDF given beamforming $f_{x,w}$ Candidate beams in θ and φ <th>$\theta_{3dB}, \varphi_{3dB}$</th> <th>3-dB beamwidth in azimuth, elevation</th>	$\theta_{3dB}, \varphi_{3dB}$	3-dB beamwidth in azimuth, elevation
EElectric field Z_0 Free-space impedance P_d Power density g Antenna gain P_r Received power h_a Aerial radiation pattern (UAV) h_a Static radiation pattern (Ground)Beamforming Training Parameters $A_{dsw} \cdot \Delta_{qsw}$ $A_{dsw} \cdot \Delta_{qsw}$ Beam-sweeping angular range $\delta_{dsw} \cdot \delta_{qsw}$ Beam-sweeping angular resolutionUAV tocordinate { $x, y, z, roll, pitch, yaw$ } i UAV coordinate { $x, y, z, roll, pitch, yaw$ } i Polar coordinate { r, θ, φ } Δ_{j}, Δ_i Hovering displacement in coord. j over i μ_{Δ_j} Mean vale of displacement in j σ_{Δ} Variance of displacement in j $f(\Delta_i)$ PDF of displacement in j f_{Δ_i} UAV coordinate 2PDF of displacement in i $\delta_{(\Delta_i)}$ Dirac delta function for displacement in i $O(\Delta_i)$ Dirac delta function for displacement in i $O(\Delta_i)$ Dirac delta function loss L_{Arr} UAV airframe-related loss L_{Hov} Hovering-related loss L_{Hov} Hovering-related loss L_{Misal} Beam misalignment loss L_{Δ_i} Distance d fluctuation loss L_{Arr} Cotal link loss σ_r, φ_T Transmitter steering angles $f_r(\theta), f_r(\varphi)$ Tx PDF to sweep in certain angle $f_k(\theta), f_k(\varphi)$ Ty PDF to sweep in certain angle $f_k(\theta), f_k(\varphi)$ Loss caused by UAV displacement in i C_{ausil} Condidate be	$\theta_{bs}, \varphi_{bs}$	Broadside direction in azimuth, elevation
Z_0 Free-space impedance P_d Power density P_d Antenna gain P_r Received power h_a Aerial radiation pattern (UAV) h_s Static radiation pattern (Ground)Beamforming Training Parameters $\Delta q_{sw}, \Delta \varphi_{sw}$ Beam-sweeping angular range $\delta q_{sw}, \delta q_{sw}$ Beam-sweeping angular resolutionUAV toordinate { $x, y, z, roll, pitch, yaw$ } i Polar coordinate { r, θ, φ } Δ_j, Δ_i Hovering displacement in dimensions i, j $A_{i,j}$ Projection of displacement in j σ_{Δ_j} Variance of displacement in j $f(\Delta_j)$ PDF of displacement in i $f_{i,j}(\Delta_i)$ DDF of displacement in i $f_{i,j}(\Delta_i)$ DDF of displacement in i $f_{i,j}(\Delta_i)$ Distance between transmitter and receiver L_{FSPL} Free Space Path Loss L_{Afr} UAV airframe-related loss L_{arov} Hovering-related loss L_{arov} Houreing-related loss L_{arov} Total link loss σ_r, φ_T Transmitter steering angles σ_r, φ_T Transmitter steering angles $f_r(\theta), f_r(\varphi)$ Rx PDF to sweep in certain angle $f_r(\theta), f_r(\varphi)$ Rx beering PDF given beamforming f_{xv} Laudidate beams in θ and φ U, V Total link loss P_{arod} Subset of candidate beams in θ and φ f_{arod} Subset of candidate beams in θ and φ $f_r(\theta), f_r(\varphi), L_{Tx}(\Delta_{\varphi})$ Lustering PDF given beamformin	E	Electric field
P_{d} Power density g g Antenna gain P_{r} R_{c} Received power h_{a} Artial radiation pattern (UAV) h_{s} Static radiation pattern (Ground)Beamforming Training Parameters $\Delta_{\theta_{SW}}, \Delta_{\varphi_{SW}}$ Beam-sweeping angular range $\delta_{\theta_{SW}}, \delta_{\psi_{SW}}$ Beam-sweeping angular range j UAV coordinate $\{x, y, z, roll, pitch, yaw\}$ i Polar coordinate $\{r, \theta, \varphi\}$ $A_{f,A}$ Hovering displacement in dimensions i, j $\Delta_{f,A}$ Hovering displacement in j $\sigma_{A_{i}}^{T}$ Variance of displacement in j $f(\Delta_{j})$ PDF of displacement in j $f_{i}(\omega)$ DDF of displacement in j $f_{i}(\omega)$ DDF of displacement in i $\delta(\Delta_{i})$ Dirac cleft function for displacement in i $\delta(\Delta_{i})$ Dirac between transmitter and receiver L_{FSPL} Free Space Path Loss L_{Afr} UAV airframe-related loss L_{arr} Distance between transmitter and receiver L_{subOpt} Sub-optimal beam selection loss L_{arr} Distance d fluctuation loss L_{arr} Distance d fluctuation loss L_{arr} Total link loss θ_{T}, φ_{T} Transmitter steering angles $f_{r}(\theta), f_{r}(\varphi)$ Tx PDF to sweep in certain angle f_{sww} Rx steering PDF given beamforming f_{sw} Subset of candidate beams in θ and φ J_{sw} Subset of candidate beams in θ and φ $J_{r}(\theta), f_{r}(\varphi)$ Tx PDF to	Z_0	Free-space impedance
gAntenna gain P_r .Received power h_a Aerial radiation pattern (UAV) h_s Static radiation pattern (Ground)Beamforming Training Parameters $\delta_{dsw}, \Delta_{qsw}$ Beam-sweeping angular range $\delta_{dsw}, \Delta_{qsw}$ Beam-sweeping angular resolutionUAV tovering Model Parameters i UAV coordinate { $x, y, z, roll, pitch, yaw}$ j UAV coordinate { r, θ, φ } Δ_{j, Δ_i} Polar coordinate { r, θ, φ } $\Delta_{i(j)}$ Projection of displacement in dimensions i, j $\sigma_{\Delta_j}^{\lambda}$ Wariance of displacement in j $\sigma_{\Delta_j}^{\lambda}$ Variance of displacement in j $f(\Delta_i)$ PDF of displacement in i $f(\Delta_i)$ Dirac delta function for displacement in i $\delta(\Delta_i)$ Dirac delta function for displacement in i $\delta(\Delta_i)$ Distance between transmitter and receiver L_{FSPL} Free Space Path Loss L_{Ar} Distance d fluctuation loss L_{Ar} Distance d fluctuation loss L_{Ar} Distance d fluctuation loss L_{rot} Total link loss σ_r, φ_R Receiver steering angles $f_R(\theta), f_R(\varphi)$ Rx PDF to sweep in certain angle $f_r(\theta), f_r(\varphi)$ Tx PDF to sweep in certain angle $f_r(\theta), f_r(\varphi)$ Tx Steering PDF given beamforming f_{ksw} Total candidate beams in θ and φ U, V Total candidate beams in θ and φ $f_r(\theta), f_r(\varphi)$ Subset of candidate beams in θ and φ $L_{r_x}(\Delta_{\theta}), L_{Tx}(\Delta_{\varphi})$ L_{subo	P_d	Power density
P_r Received power h_a Aerial radiation pattern (UAV) h_s Static radiation pattern (Ground)Beamforming Training Parameters Δq_{5W} , $\Delta \varphi_{5W}$ Beam-sweeping angular range δq_{5W} , δq_{5W} Beam-sweeping angular resolutionUAV Hovering Model Parameters i UAV coordinate { $x, y, z, roll, pitch, yaw$ } i Polar coordinate { r, θ, φ } $A_{i,j}$ Projection of displacement in dimensions i, j Δ_{j,Δ_i} Hovering displacement in j $\sigma_{A_j}^{-}$ Variance of displacement in j $f(\Delta_j)$ PDF of displacement in j $f_i(\Delta_i)$ Unnormalized PDF of displacement in i $f_{i,(\Delta_i)}$ Unnormalized PDF of displacement in i $f_{i,(\Delta_i)}$ Unnormalized PDF of displacement in i $Channel Model Parameters$ Tree Space Path Loss L_{Afr} UAV airframe-related loss L_{Hov} Hovering-related loss L_{Misal} Beam misalignment loss L_{A_fr} Distance d fluctuation loss L_{Arr} Distance d fluctuation loss L_{Arr} Transmitter stering angles $f_r(\theta), f_r(\varphi)$ Tx PDF to sweep in certain angle $f_{r,\Theta}(\theta), f_R(\varphi)$ Rx PDF to sweep in certain angle f_{rsw} Rx steering PDF given beamforming f_{rsw} Rx steering PDF given beamforming f_{rsw} Subset of candidate beams (u, v) L_{A_i} Lsubopt at transmitter given pair (u, v) $L_{rx}(\theta_n), L_{rx}(\Delta_{\varphi})$ Lsubopt at massing met loss <t< th=""><th>g</th><th>Antenna gain</th></t<>	g	Antenna gain
$\begin{array}{lll} \begin{array}{lll} h_{s} & \operatorname{Aerial radiation pattern (UAV)} \\ h_{s} & \operatorname{Static radiation pattern (Ground)} \\ \hline \\ $	P_r	Received power
n_s Statuc ration pattern (Ground)Beamforming Training Parameters $\Delta q_{SW}, \Delta_{\varphi SW}$ Beam-sweeping angular range $\delta_{g_{SW}}, \delta_{\varphi_{SW}}$ Beam-sweeping angular resolution UAV coordinate $\{x, y, z, roll, pitch, yaw\}$ i Polar coordinate $\{x, y, z, roll, pitch, yaw\}$ j UAV coordinate $\{x, y, z, roll, pitch, yaw\}$ i Polar coordinate $\{x, y, z, roll, pitch, yaw\}$ $\lambda_{i(j)}$ Projection of displacement in coord. j over i M_{Δ_j} Mean vale of displacement in j $\sigma_{\Delta_j}^2$ Variance of displacement in j $f(\Delta_i)$ PDF of displacement in j $f_{id}(\Delta_i)$ DDF of displacement in j $f_{id}(\Delta_i)$ Unnormalized PDF of displacement in i $\delta(\Delta_i)$ Distance between transmitter and receiver L_{FSPL} Free Space Path Loss L_{Afr} UAV airframe-related loss L_{afr} UAV airframe-related loss L_{afr} Distance d fluctuation loss L_{afr} Distance d fluctuation loss L_{afr} Transmitter steering angles f_r, φ_T Transmitter steering angles $f_r, (\varphi), f_R(\varphi)$ Tx PDF to sweep in certain angle $f_R(\theta), f_R(\varphi)$ Kx steering PDF given beamforming f_{xy} Candidate beams in θ and φ U, V Total candidate beams in θ and φ U_{aff} <t< th=""><th>n_a h</th><th>Aerial radiation pattern (UAV)</th></t<>	n _a h	Aerial radiation pattern (UAV)
$ \begin{array}{c c c c c c c c c c c c c c c c c c c $	Raamforming Tusining	Darameters
$ \begin{aligned} \Delta_{fgwv}, \Delta_{\varphi SW} & \text{Deam-Sweeping angular range} \\ \hline \delta_{\partial_{Gwv}}, \delta_{\varphi_{SW}} & \text{Beam-Sweeping angular resolution} \\ \hline UAV Hovering Model Parameters \\ \hline i & Polar coordinate {x, y, z, roll, pitch, yaw} \\ \hline i & Polar coordinate {r, \theta, \varphi} \\ \Delta_{j}, \Delta_{i} & \text{Hovering displacement in dimensions } i, j \\ \Delta_{i(j)} & Projection of displacement in coord. j over i \\ \mu_{\Delta_{j}} & Mean vale of displacement in j \\ \hline f(\Delta_{j}) & PDF of displacement in j \\ f(\Delta_{i}) & PDF of displacement in j \\ f_{ii}(\Delta_{i}) & DDF of displacement in j \\ f_{ii}(\Delta_{i}) & DDr of displacement in j \\ f_{ii}(\Delta_{i}) & Dirac delta function for displacement in i \\ \hline o (\Delta_{i}) & Dirac delta function for displacement in i \\ \hline Channel Model Parameters \\ \hline d & Distance between transmitter and receiver \\ L_{FSPL} & Free Space Path Loss \\ L_{Afr} & UAV airframe-related loss \\ L_{Mov} & Hovering-related loss \\ L_{Air} & Distance d fluctuation loss \\ L_{Tor} & Total link loss \\ \phi_{T}, \phi_{T} & Transmitter steering angles \\ f_{T}(\theta), f_{T}(\phi) & X PDF to sweep in certain angle \\ f_{R}(\theta), f_{R}(\phi) & Rx PDF to sweep in certain angle \\ f_{R}(\theta), f_{R}(\phi) & Rx steering PDF given beamforming \\ u, v & Candidate beams in \theta and \phi \\ S & Subset of candidate beams in \theta and \phi \\ S & Subset of Causing a given pair (u, v) \\ L_{Tx}(\Delta_{\theta}), L_{Tx}(\Delta_{\varphi}) & L_{SubOpt} \\ Loss caused by UAV displacement in i \\ C & Set of all possible combinations of \Delta_{i} \\ S & Subset of C causing a given pair (u, v) \\ L_{Tx}(\Delta_{\theta}), L_{Tx}(\Delta_{\varphi}) & L_{SubOpt} \\ Loss caused by UAV displacement in i \\ C & Set of all possible combinations of \Delta_{i} \\ S & Subset of C causing a given loss \\ Y_{th} & Threshold for stochastic loss estimation \\ Algorithm Parameters \\ W_{k}(\Delta_{i}) & Confidence veight, pair k, dimension i \\ w_{L}(\Delta_{i}) & Confidence veight, pair k, dimension i \\ pow_{k} & Measured power pair of beams k \\ ts & Time-stamped \\ t_{sweep} & Beam-sweeping time \\ M & Location samples collected during t_{sweep} \\ H & Mapping matrix (Pow_k, UAV_{x,y,z}) \\ \end{cases}$		Ream-swooping angular range
0_{dgsw} Deamistic equal resolution UAV Hovering Model Parameters i UAV coordinate $\{x, y, z, roll, pitch, yaw\}$ i Polar coordinate $\{r, \theta, \varphi\}$ Δ_j, Δ_i Hovering displacement in coord. j over i μ_{Δ_j} Mean vale of displacement in $coord. j$ over i μ_{Δ_j} Mean vale of displacement in j $\sigma_{\Delta_j}^2$ Variance of displacement in j $f(\Delta_i)$ PDF of displacement in j $f_{ai}(\Delta_i)$ Unnormalized PDF of displacement in i $\delta(\Delta_i)$ Dirac delta function for displacement in i $Channel Model Parameters$ Tree Space Path Loss L_{Afr} UAV airframe-related loss L_{Afr} UAV airframe-related loss L_{Misal} Beam misalignment loss L_{Misal} Beam misalignment loss L_{Δ_r} Distance d fluctuation loss L_{Arr} Distance d fluctuation loss L_{Arr} Distance d fluctuation loss L_{Arr} Transmitter steering angles θ_R, φ_R Receiver steering angles $f_r(\theta), f_R(\varphi)$ Tx PDF to sweep in certain angle f_{rsw} Tx steering PDF given beamforming f_{Rsw} Restering PDF given beamforming f_{Rsw} Candidate beams in θ and φ U, V Total combination of candidate beams $f_r(\theta_i), L_{Tx}(\Phi_{\varphi})$ L_{SubOpt} at transmitter given pair (u, v) L_{rsw} Candidate beams in θ and φ $f_r(\theta_i), L_{Tx}(\Delta_{\varphi})$ L_{Misal} for hovering displacement $\Delta_i, \Delta_{\varphi}$ L_{Ai} Confid	$\Delta_{\theta_{SW}}, \Delta_{\varphi_{SW}}$	Beam-sweeping angular range
iUAV coordinate {x, y, z, roll, pitch, yaw}jUAV coordinate {x, y, z, roll, pitch, yaw} Δ_i, Δ_i Hovering displacement in dimensions i, j $\Delta_{i(j)}$ Projection of displacement in coord. j over i μ_{Δ_j} Mean vale of displacement in j $\sigma_{\Delta_j}^2$ Variance of displacement in j $f(\Delta_j)$ PDF of displacement in i $f_{i(d_i)}$ Unnormalized PDF of displacement in i $\delta(\Delta_i)$ Dirac delta function for displacement in i $\delta(\Delta_i)$ Dirac delta function for displacement in iChannel Model ParametersDistance between transmitter and receiver L_{FSPL} Free Space Path Loss L_{Afr} UAV airframe-related loss L_{Hov} Hovering-related loss L_{Misal} Beam misalignment loss L_{Δ_r} Distance d fluctuation loss L_{Ar} Distance d fluctuation loss L_{Ar} Total link loss θ_r, φ_R Receiver steering angles $\theta_r(\phi), f_r(\varphi)$ Tx PDF to sweep in certain angle $f_r(\theta), f_r(\varphi)$ Rx PDF to sweep in certain angle $f_r(\theta_i), f_R(\varphi)$ LsubOpt Given beamforming M_{Swew} Rx steering PDF given beamforming f_{rsw} Total combination of candidate beams u, v Candidate beams in θ and φ S Subset of candidate beams in θ and φ $f_r(\theta_i), L_{Tx}(\Delta_{\phi})$ L_{SubOpt} at transmitter given pair (u, v) $T_{rs}(\Delta_{\theta_i}), L_{Tx}(\Delta_{\phi_i})$ Confidence-cost weight, pair k , dimension i $v_L_{A_i}$ Confidence weight, pair	$\frac{\sigma_{\theta_{SW}}, \sigma_{\varphi_{SW}}}{11AV Hovering Model}$	Parameters
$\begin{array}{ccc} j & constraints [cr, g, \varphi] (w), (w), pinch ginds fit of a point coordinate [cr, g, \varphi] \\ \Delta_j, \Delta_i & Hovering displacement in dimensions i, j \\ \Delta_{i(j)} & Projection of displacement in coord. j over i \\ \mu_{\Delta_j} & Mean vale of displacement in j \\ f(\Delta_j) & PDF of displacement in j \\ f(\Delta_i) & DDF of displacement in j \\ f_{ii}(\Delta_i) & Unnormalized PDF of displacement in i \\ \delta(\Delta_i) & Dirac delta function for displacement in i \\ \delta(\Delta_i) & Dirac delta function for displacement in i \\ \delta(\Delta_i) & Dirac delta function for displacement in i \\ \delta(\Delta_i) & Dirac delta function for displacement in i \\ \delta(\Delta_i) & Dirac delta function for displacement in i \\ \delta(\Delta_i) & Dirac delta function for displacement in i \\ \delta(\Delta_i) & Dirac delta function for displacement in i \\ \delta(\Delta_i) & Dirac delta function for displacement in i \\ \delta(\Delta_i) & Dirac delta function for displacement in i \\ \delta(\Delta_i) & Dirac delta function for displacement in i \\ \delta(\Delta_i) & Dirac delta function for displacement in i \\ \delta(\Delta_i) & Dirac delta function for displacement in i \\ \delta(\Delta_i) & Dirac delta function for displacement in i \\ \delta(\Delta_i) & Dirac delta function for displacement in i \\ \delta(\Delta_i) & Dirac delta function for displacement in i \\ \delta(\Delta_i) & Dirac delta function for displacement in i \\ SubOpt & Sub-optimal beam selection loss \\ L_{Ar} & Distance d fluctuation loss \\ L_{Ar} & Distance d fluctuation loss \\ L_{Ar} & Distance d fluctuation loss \\ f_{T}(\varphi), f_{T}(\varphi) & Tx PDF to sweep in certain angle \\ f_{R}(\theta), f_{R}(\varphi) & Rx PDF to sweep in certain angle \\ f_{R}(\theta), f_{R}(\varphi) & Rx PDF to sweep in certain angle \\ f_{rsw} & Rx steering PDF given beamforming \\ f_{rsw} & Tx steering PDF given beamforming \\ h_{s} & Subset of candidate beams (u, v) \\ N_{b} & Total combination of candidate beams \\ L_{Tx}(\Delta_{\theta}), L_{Tx}(\Delta_{\varphi}) & L_{Misal} for hovering displacement in i \\ C & Set of all possible combinations of \Delta_i \\ Q & Subset of C causing a given loss \\ Y_{th} & Threshold for stochastic loss estimation \\ Algorithm Parameters \\ w_k(\Delta_i) & Confidence weight, pair k, dimension i \\ pow_k$	i	UAV coordinate $\{x, y, z \text{ roll nitch } yazu\}$
$\begin{array}{cccc} \lambda_{j}, \Delta_{i} & Hovering displacement in dimensions i, j \\ \lambda_{i(j)} & Projection of displacement in coord. j over i \\ \mu_{\Delta_{j}} & Mean vale of displacement in j \\ \sigma_{\Delta_{j}}^{2} & Variance of displacement in j \\ f(\Delta_{j}) & PDF of displacement in i \\ f_{i}(\Delta_{i}) & DDF of displacement in j \\ f_{u_{l}}(\Delta_{i}) & Unnormalized PDF of displacement in i \\ \hline \delta(\Delta_{i}) & Dirac delta function for displacement in i \\ \hline Channel Model Parameters \\ \hline d & Distance between transmitter and receiver \\ L_{FSPL} & Free Space Path Loss \\ L_{Afr} & UAV airframe-related loss \\ L_{Hov} & Hovering-related loss \\ L_{Mov} & Hovering-related loss \\ L_{Mov} & Hovering-related loss \\ L_{Mov} & Distance d fluctuation loss \\ L_{Misal} & Beam misalignment loss \\ L_{A_{r}} & Distance d fluctuation loss \\ L_{rot} & Total link loss \\ \theta_{T}, \varphi_{T} & Transmitter steering angles \\ \theta_{R}, \varphi_{R} & Receiver steering angles \\ f_{R}(\theta), f_{R}(\varphi) & Tx PDF to sweep in certain angle \\ f_{rsw} & Rx steering PDF given beamforming \\ f_{rsw} & Rx steering PDF given beamforming \\ f_{rsw} & Rx steering PDF given beamforming \\ h_{v} & Candidate beams (u, v) \\ N_{b} & Total candidate beams (u, v) \\ M_{r}_{x}(\Delta_{\theta_{i}}), L_{Tx}(\varphi_{v}) & L_{Misal} for hovering displacement \lambda_{\theta}, \Delta_{\varphi} \\ L_{\Delta_{i}} & Loss caused by UAV displacement in i \\ G & Subset of candidate beams (u, v) \\ M_{Fx}(\Delta_{\theta_{i}}), L_{Tx}(\varphi_{v}) & L_{Misal} for hovering displacement in i \\ C & Set of all possible combinations of \Delta_{i} \\ Q & Subset of C causing a given loss \\ f_{rk}(\Delta_{i}) & Confidence veight, pair k, dimension i \\ measured power pair of beams k \\ Time-stamped \\ t_{sweep} & Beam-sweeping time \\ M & Location samples collected during t_{sweep} \\ H & Mapping matrix (pow_k, UAV_{x,y,z}) \\ \end{array}$	j i	Polar coordinate $\{r, \theta, \varphi\}$
$\begin{array}{cccc} Projection of displacement in coord. j over i\\ \mu_{A_j} & Mean vale of displacement in j\\ \sigma_{A_i}^{(j)} & PDF of displacement in j\\ f(\Delta_i) & PDF of displacement in i\\ f_i(\Delta_i) & DDF of displacement in j\\ f_{ai}(\Delta_i) & Unnormalized PDF of displacement in i\\ \hline f_{ai}(\Delta_i) & Distance between transmitter and receiver\\ \hline f_{FSPL} & Free Space Path Loss\\ L_{A_ir} & UAV airframe-related loss\\ L_{Hov} & Hovering-related loss\\ L_{Mov} & Hovering-related loss\\ L_{Mov} & Hovering-related loss\\ L_{A_ir} & Distance d fluctuation loss\\ L_{A_ir} & Distance d fluctuation loss\\ L_{A_ir} & Transmitter steering angles\\ \theta_R, \varphi_R & Receiver steering angles\\ f_r(\theta), f_R(\varphi) & Rx PDF to sweep in certain angle\\ f_{SW} & Rx steering PDF given beamforming\\ H_x v & Candidate beams in \theta and \varphi\\ U, V & Total candidate beams in \theta and \varphi\\ U, V & Total combination of candidate beams\\ L_{Tac}(\theta_u), L_{Tx}(\phi_v) & L_{SubOpt} at transmitter given pair (u, v)\\ L_{Tx}(\Delta_{\theta}), L_{Tx}(\phi_{\varphi}) & Subsopt at transmitter given pair (u, v)\\ L_{Misal} & Real transmitter given pair (u, v)\\ L_{Misal} & Real transmitter given pair (u, v)\\ L_{Misal} & Real transmitter given pair (u, v)\\ L_{Tx}(\Delta_{\theta}), L_{Tx}(\phi_{\varphi}) & L_{SubOpt} at transmitter given pair (u, v)\\ L_{Misal} for hovering displacement in i\\ C & Set of all possible combination of \Delta_iSubset of C ausing a given lossT_{Th} & Threshold for stochastic loss estimation\\ Algorithm Parameters & w_k(\Delta_i) & Confidence weight, pair k, dimension i\\ pow_k & Measured power pair of beams k\\ ts & Time-stamped\\ t_{sweep} & Beam-sweeping time\\ M & Location samples collected during t_{sweep}\\ H & Mapping matrix (pow_k, UAV_{x,y,z}) & \\ \end{array}$	Λ_{i}, Λ_{i}	Hovering displacement in dimensions <i>i</i> , <i>i</i>
$\begin{array}{cccc} \mu_{\Delta_j} & \text{Mean vale of displacement in } j \\ \sigma_{\Delta_j}^2 & \text{Variance of displacement in } j \\ f(\Delta_j) & \text{PDF of displacement in } i \\ f_i(\Delta_i) & \text{PDF of displacement in } j \\ f_{u_i}(\Delta_i) & \text{Unnormalized PDF of displacement in } i \\ \delta(\Delta_i) & \text{Dirac delta function for displacement in } i \\ \hline Channel Model Parameters \\\hline d & \text{Distance between transmitter and receiver} \\ L_{FSPL} & Free Space Path Loss \\ L_{Afr} & UAV airframe-related loss \\ L_{Hov} & Hovering-related loss \\ L_{Misal} & \text{Beam misalignment loss} \\ L_{A_r} & \text{Distance } d \text{fluctuation loss} \\ d_{T,\sigma} & \text{Total link loss} \\ \theta_{T,\varphi_T} & \text{Transmitter steering angles} \\ \theta_{R,\varphi_R} & \text{Receiver steering angles} \\ f_r(\theta), f_r(\varphi) & \text{Tx PDF to sweep in certain angle} \\ f_{Tsw} & \text{Tx steering PDF given beamforming} \\ f_{Rsw} & \text{Rx steering PDF given beamforming} \\ u, v & \text{Candidate beams in } \theta \text{ and } \varphi \\ S & \text{Subset of candidate beams } (u, v) \\ N_b & \text{Total combination of candidate beams} \\ L_{Tx}(\Phi_u), L_{Tx}(\Phi_{\varphi}) & L_{SubOpt} \\ Loss caused by UAV displacement in i \\ C & Set of all possible combinations i \Delta_i, \Delta_{\varphi} \\ L_{A_i} & \text{Loss caused by UAV displacement in i} \\ M_{Loss caused by UAV displacement in i \\ C & Set of all possible combinations i \Delta_i, \Delta_{\varphi} \\ L_{A_i} & \text{Loss caused by UAV displacement in i} \\ C & Set of all possible combinations i \Delta_i, \Delta_{\varphi} \\ L_{A_i} & \text{Loss caused by UAV displacement in i} \\ C & Set of all possible combinations i \Delta_i, \Delta_{\varphi} \\ L_{A_i} & \text{Loss caused by UAV displacement in i} \\ C & \text{Set of all possible combinations i} \\ M_{Location samples} & \text{Collected during } t_{sweep} \\ H & \text{Mapping matrix} (paw_k, UAV_{x,y,z}) \\ H^* & \text{Proposed pair of beams \\ F^* & \text{Proposed pair of beams} \\ $	$\Delta_{i(i)}$	Projection of displacement in coord. <i>i</i> over <i>i</i>
$T_{\Delta_i}^2$ Variance of displacement in j $f(\Delta_i)$ PDF of displacement in i $f_i(\Delta_i)$ PDF of displacement in i $\delta(\Delta_i)$ Dirac delta function for displacement in i $\delta(\Delta_i)$ Dirac delta function for displacement in i $Channel Model Parameters$ Channel Model Parameters d Distance between transmitter and receiver L_{FSPL} Free Space Path Loss L_{Hov} Hovering-related loss L_{Hov} Hovering-related loss L_{Misal} Beam misalignment loss L_{Δ_r} Distance d fluctuation loss L_{Tot} Total link loss θ_r, φ_R Receiver steering angles θ_r, φ_R Receiver steering angles $f_r(\theta), f_R(\varphi)$ Tx PDF to sweep in certain angle f_{rsw} Tx steering PDF given beamforming f_{Rsw} Ka steering PDF given beamforming m_v Candidate beams in θ and φ U, V Total candidate beams (u, v) N_b Total combination of candidate beams $L_{Tx}(\theta_u), L_{Tx}(\phi_v)$ L_{SubOpt} at transmitter given pair (u, v) $L_{Tx}(\Delta_{\theta}), L_{Tx}(\Delta_{\varphi})$ L_{Misal} for hovering displacement in i C Set of all possible combinations of Δ_i Ω Subset of C causing a given loss γ_{th} Threshold for stochastic loss estimation $A_{\thetax}(\Delta_i)$ Confidence-cost weight, pair k , dimension i pow_k Measured power pair of beams k t_{xweep} Beam-sweeping time M Location samples collec	μ_{Λ}	Mean vale of displacement in i
$\begin{array}{cccc} & & & & & \\ f(\Delta_i) & & & & & & \\ PDF of displacement in i \\ f_i(\Delta_i) & & & & & \\ PDF of displacement in i \\ \hline f_{wl}(\Delta_i) & & & & \\ Dirac delta function for displacement in i \\ \hline \hline channel Model Parameters \\\hline d & & & & \\ Distance between transmitter and receiver \\\hline L_{FSPL} & & & \\ Free Space Path Loss \\\hline L_{Afr} & & & & \\ UAV airframe-related loss \\\hline L_{Hov} & & & & \\ Hovering-related loss \\\hline L_{Mov} & & & \\ Hovering-related loss \\\hline L_{Misal} & & & \\ Beam misalignment loss \\\hline L_{A_c} & & & \\ Distance d fluctuation loss \\\hline L_{Tot} & & & \\ Total link loss \\\hline \theta_r, \varphi_T & & & \\ Transmitter steering angles \\\hline \theta_R, \varphi_R & & & \\ Receiver steering angles \\\hline f_R(\theta), f_R(\varphi) & & \\ Tx PDF to sweep in certain angle \\f_R(\theta), f_R(\varphi) & & \\ Tx PDF to sweep in certain angle \\f_R(\theta), f_R(\varphi) & & \\ Tx steering PDF given beamforming \\\hline f_{rsw} & & \\ Tx steering PDF given beamforming \\\hline f_{rsw} & & \\ Total candidate beams in \theta and \varphi \\\hline U, V & & \\ Total combination of candidate beams (u, v) \\\hline N_b & & \\ Total combination of candidate beams \Delta_{\theta}, \Delta_{\varphi} \\\hline L_{\Delta_i} & & \\ Loss caused by UAV displacement in i \\\hline C & \\ Set of all possible combinations of \Delta_i \\\hline \Omega & & \\ Subset of C acusing a given loss \\\hline f_{r(A_i)} & & \\ Confidence-cost weight, pair k, dimension i \\\hline m_{V_k}(\Delta_i) & \\ Confidence-cost weight, pair k, dimension i \\\hline m_{V_k}(\Delta_i) & \\ formitare stamped \\\hline f_{sweep} & \\ Beam-sweeping time \\\hline M & \\ Location samples collected during t_{sweep} \\\hline H & \\ Mapping matrix (pow_k, UAV_{x,y,z}) \\\hline k^* & & \\ Proposed pair of beams \\\hline \end{array}$	σ^2	Variance of displacement in i
$\begin{array}{cccc} f_1(\Delta_i) & \text{PDF of displacement in } i \\ f_{iu}(\Delta_i) & \text{PDF of displacement in } i \\ \hline f_{iu}(\Delta_i) & \text{Unnormalized PDF of displacement in } i \\ \hline Channel Model Parameters \\ \hline d & \text{Distance between transmitter and receiver} \\ \hline L_{FSPL} & \text{Free Space Path Loss} \\ \hline L_{Afr} & \text{UAV airframe-related loss} \\ \hline L_{Hov} & \text{Hovering-related loss} \\ \hline L_{Hov} & \text{Hovering-related loss} \\ \hline L_{Hov} & \text{Hovering-related loss} \\ \hline L_{Mov} & \text{Beam misalignment loss} \\ \hline L_{Tot} & \text{Distance } d \text{ fluctuation loss} \\ \hline L_{Tot} & \text{Total link loss} \\ \hline \theta_{T}, \varphi_{T} & \text{Transmitter steering angles} \\ \hline \theta_{R}, \varphi_{R} & \text{Receiver steering angles} \\ f_{T}(\theta), f_{T}(\varphi) & \text{Tx PDF to sweep in certain angle} \\ f_{R}(\theta), f_{R}(\varphi) & \text{Rx PDF to sweep in certain angle} \\ f_{Rsw} & \text{Tx steering PDF given beamforming} \\ f_{Rsw} & \text{Rx steering PDF given beamforming} \\ u, v & \text{Candidate beams in } \theta \text{ and } \varphi \\ S & \text{Subset of candidate beams in } \theta \text{ and } \varphi \\ S & \text{Subset of candidate beams in } \theta \text{ and } \varphi \\ L_{\Delta_i} & \text{Loss caused by UAV displacement in } i \\ C & \text{Set of all possible combinations of } \Delta_i \\ \Omega_{\Delta_i} & \text{Subset of C ausing a given loss} \\ \frac{I_{Lx}(\Delta_i)}{I_{Tx}(\Delta_{\varphi})} & \text{Confidence weight, pair k, dimension i \\ Measured power pair of beams k \\ ts & \text{Time-stamped} \\ t_{sweep} & \text{Beam-sweeping time} \\ M & \text{Location samples collected during } t_{sweep} \\ M & \text{Mapping matrix} (pow_k, UAV_{x,y,z}) \\ k^* & \text{Proposed pair of beams} \end{cases}$	$\int \Delta_j f(\Lambda_j)$	PDF of displacement in i
$ \begin{array}{cccc} & \text{Hor ormalized PDF of displacement in } i \\ \hline f_{u}(\Delta_i) & \text{Unnormalized PDF of displacement in } i \\ \hline Channel Model Parameters \\ \hline d & \text{Distance between transmitter and receiver} \\ \hline L_{FSPL} & Free Space Path Loss \\ \hline L_{Afr} & UAV airframe-related loss \\ \hline L_{Hov} & Hovering-related loss \\ \hline L_{Hov} & Sub-optimal beam selection loss \\ \hline L_{Misal} & Beam misalignment loss \\ \hline L_{Tot} & Total link loss \\ \hline \theta_{T}, \varphi_{T} & Transmitter steering angles \\ \hline f_{R}(\theta), f_{R}(\varphi) & Rx PDF to sweep in certain angle \\ \hline f_{Rsw} & Rx steering PDF given beamforming \\ \hline R_{xsw} & Rx steering PDF given beamforming \\ \hline R_{x}(\theta_u), L_{Tx}(\varphi_v) & L_{SubOpt} at transmitter given pair (u, v) \\ \hline L_{Tx}(\Delta_{\theta}), L_{Tx}(\varphi_v) & L_{SubOpt} at transmitter given pair (u, v) \\ \hline L_{Tx}(\Delta_{\theta}), C_{Tx}(\Delta_{\varphi}) & L_{Misal} \\ \hline One constant of constant of constant of constant angle \\ \hline f_{Rsw} & Rx steering displacement in i \\ \hline C & Set of all possible combinations of \Delta_i \\ \hline \Omega & Subset of candidate beams (u, v) \\ \hline N_{b} & Total combination of candidate beams \\ \hline L_{Ai} & Loss caused by UAV displacement in i \\ \hline C & Set of all possible combinations of \Delta_i\Omega & Subset of C causing a given loss \\ \hline \gamma_{th} & Threshold for stochastic loss estimation \\ \hline Algorithm Parameters \\ \hline w_k(\Delta_i) & Confidence weight, pair k, dimension i \\ \hline pow_k & Measured power pair of beams k \\ ts & Time-stamped \\ \hline t_{sweep} & Beam-sweeping time \\ \hline M & Location samples collected during t_{sweep} \\ \hline H & Mapping matrix (pow_k, UAV_{x,y,z}) \\ \hline rel \\ \hline \end{array}$	$f_i(\Delta_j)$	PDF of displacement in <i>i</i>
$\begin{array}{llllllllllllllllllllllllllllllllllll$	$f_{iii}(\Delta_i)$	Unnormalized PDF of displacement in <i>i</i>
Channel Model ParametersdDistance between transmitter and receiver L_{FSPL} Free Space Path Loss L_{Afr} UAV airframe-related loss L_{Afr} UAV airframe-related loss L_{Misal} Beam misalignment loss L_{Misal} Beam misalignment loss L_{Tot} Total link loss θ_r, φ_R Receiver steering angles θ_r, φ_R Receiver steering angles $f_r(\theta), f_r(\varphi)$ Tx PDF to sweep in certain angle f_{Rsw} Rx steering PDF given beamforming f_{Rsw} Rx steering PDF given beamforming u, v Candidate beams in θ and φ U, V Total combination of candidate beams u, v Candidate beams (u, v) N_b Total combination of candidate beams $L_{T_x}(\Delta_{\theta}), L_{T_x}(\Delta_{\varphi})$ L_{Misal} for hovering displacements $\Delta_{\theta}, \Delta_{\varphi}$ L_{Δ_i} Confidence weight, pair k , dimension i Q Subset of C causing a given loss γ_{th} Threshold for stochastic loss estimation $Algorithm Parameters$ Measured power pair of beams k ts Time-stamped t_{sweep} Beam-sweeping time M Location samples collected during t_{sweep} H Mapping matrix $(pow_k, UAV_{x,y,z})$ k^* Proposed pair of beams	$\delta(\Delta_i)$	Dirac delta function for displacement in <i>i</i>
$\begin{array}{lll} d & \mbox{Distance between transmitter and receiver} \\ L_{FSPL} & \mbox{Free Space Path Loss} \\ L_{Afr} & \mbox{UAV airframe-related loss} \\ L_{Hov} & \mbox{Hovering-related loss} \\ L_{Hov} & \mbox{Hovering-related loss} \\ L_{SubOpt} & \mbox{Sub-optimal beam selection loss} \\ L_{SubOpt} & \mbox{Sub-optimal beam selection loss} \\ L_{A_r} & \mbox{Distance } d \mbox{fluctuation loss} \\ L_{Tot} & \mbox{Total link loss} \\ \theta_T, \varphi_T & \mbox{Transmitter steering angles} \\ \theta_R, \varphi_R & \mbox{Receiver steering angles} \\ f_T(\theta), f_T(\varphi) & \mbox{Tx PDF to sweep in certain angle} \\ f_{R}(\theta), f_R(\varphi) & \mbox{Rx PDF to sweep in certain angle} \\ f_{Rsw} & \mbox{Rx steering PDF given beamforming} \\ models & \mbox{Rx steering PDF given beamforming} \\ models & \mbox{Rx steering PDF given beamforming} \\ u, v & \mbox{Candidate beam indices in } \theta \mbox{ and } \varphi \\ U, V & \mbox{Total candidate beams in (u, v)} \\ N_b & \mbox{Total candidate beams in (u, v)} \\ N_b & \mbox{Total candidate beams (u, v)} \\ N_b & \mbox{Total candidate beams (u, v)} \\ M_b & \mbox{Total candidate beams (u, v)} \\ L_{Tx}(\Delta_{\theta}), L_{Tx}(\Delta_{\varphi}) & \mbox{LsubOpt at transmitter given pair (u, v)} \\ L_{A_i} & \mbox{Loss caused by UAV displacement in i \\ C & \mbox{Set of all possible combinations of Δ_i} \\ \Omega & \mbox{Subset of C causing a given loss γ_{th} \\ \hline Threshold for stochastic loss estimation i \\ \hline M_{Location samples collected during t_{sweep} \\ \hline H & \mbox{Mapping matrix} $(pow_k, UAV_{x,y,z})$ \\ k^* & \mbox{Proposed pair of beams} $$	Channel Model Parame	eters
$\begin{array}{lll} L_{FSPL} & \mbox{Free Space Path Loss} \\ L_{Afr} & \mbox{UAV airframe-related loss} \\ L_{Hov} & \mbox{Hovering-related loss} \\ L_{Hov} & \mbox{Hovering-related loss} \\ L_{SubOpt} & \mbox{Sub-optimal beam selection loss} \\ L_{SubOpt} & \mbox{Sub-optimal beam selection loss} \\ L_{\Delta_r} & \mbox{Distance } d \mbox{fluctuation loss} \\ L_{Tot} & \mbox{Total link loss} \\ \theta_T, \varphi_T & \mbox{Transmitter steering angles} \\ \theta_R, \varphi_R & \mbox{Receiver steering angles} \\ f_T(\theta), f_T(\varphi) & \mbox{Tx PDF to sweep in certain angle} \\ f_{R}(\theta), f_R(\varphi) & \mbox{Rx PDF to sweep in certain angle} \\ f_{rsw} & \mbox{Tx steering PDF given beamforming} \\ h_{sw} & \mbox{Rx steering PDF given beamforming} \\ u, v & \mbox{Candidate beams in } \theta \mbox{ and } \varphi \\ U, V & \mbox{Total candidate beams in } \theta \mbox{ and } \varphi \\ S & \mbox{Subset of candidate beams } (u, v) \\ N_b & \mbox{Total combination of candidate beams} \\ L_{Tx}(\theta_u), L_{Tx}(\varphi_v) & \mbox{LsubOpt} \mbox{ at transmitter given pair } (u, v) \\ L_{Tx}(\Delta_{\theta}), L_{Tx}(\Delta_{\varphi}) & \mbox{Lmiscal for hovering displacements } \Delta_{\theta}, \Delta_{\varphi} \\ L_{\Delta_i} & \mbox{Loss caused by UAV displacement in } i \\ C & \mbox{Subset of C causing a given loss} \\ \gamma_{th} & \mbox{Threshold for stochastic loss estimation} \\ \hline Algorithm Parameters \\ \hline w_k(\Delta_i) & \mbox{Confidence-cost weight, pair k, dimension i \\ pow_k & \mbox{Measured power pair of beams k \\ ts & \mbox{Time-stamped} \\ t_{sweep} & \mbox{Beam selection samples collected during } t_{sweep} \\ H & \mbox{Mapping matrix} (pow_k, UAV_{x,y,z}) \\ k^* & \mbox{Proposed pair of beams} \\ \end{array}$	d	Distance between transmitter and receiver
$\begin{array}{lll} L_{Afr} & UAV airframe-related loss \\ L_{Hov} & Hovering-related loss \\ L_{SubOpt} & Sub-optimal beam selection loss \\ L_{Misal} & Beam misalignment loss \\ L_{\Delta_r} & Distance d fluctuation loss \\ L_{Tot} & Total link loss \\ \theta_T, \varphi_T & Transmitter steering angles \\ \theta_R, \varphi_R & Receiver steering angles \\ f_T(\theta), f_T(\varphi) & Tx PDF to sweep in certain angle \\ f_R(\theta), f_R(\varphi) & Rx PDF to sweep in certain angle \\ f_{r_{SW}} & Tx steering PDF given beamforming \\ u, v & Candidate beam indices in \theta and \varphi \\ U, V & Total candidate beams in \theta and \varphi \\ S & Subset of candidate beams (u, v) \\ N_b & Total combination of candidate beams \\ L_{Tx}(\theta_u), L_{Tx}(\varphi_v) & L_{SubOpt} at transmitter given pair (u, v) \\ L_{Tx}(\Delta_{\theta}), L_{Tx}(\Delta_{\varphi}) & L_{Misal} for hovering displacements \Delta_{\theta}, \Delta_{\varphi} \\ L_{\Delta_i} & Subset of C causing a given loss \\ \gamma_{th} & Threshold for stochastic loss estimation \\ Algorithm Parameters \\\hline w_k(\Delta_i) & Confidence weight, pair k, dimension i \\ pow_k & Measured power pair of beams k \\ ts & Time-stamped \\ t_{sweep} & Beam-sweeping time \\ M & Location samples collected during t_{sweep} \\ H & Mapping matrix (powk, UAV_{x,y,z}) \\ k^* & Proposed pair of beams \\\hline \end{tabular}$	L_{FSPL}	Free Space Path Loss
L_{Hov} Hovering-related loss L_{SubOpt} Sub-optimal beam selection loss L_{Misal} Beam misalignment loss L_{Δ_r} Distance d fluctuation loss L_{Tot} Total link loss θ_T, φ_T Transmitter steering angles θ_T, φ_R Receiver steering angles $f_T(\theta), f_T(\varphi)$ Tx PDF to sweep in certain angle $f_{R}(\theta), f_R(\varphi)$ Rx PDF to sweep in certain angle $f_{r_{SW}}$ Tx steering PDF given beamforming u, v Candidate beam indices in θ and φ U, V Total candidate beams in θ and φ S Subset of candidate beams (u, v) N_b Total combination of candidate beams $L_{Tx}(\theta_u), L_{Tx}(\varphi_v)$ L_{SubOpt} at transmitter given pair (u, v) $L_{Tx}(\Delta_{\theta}), L_{Tx}(\Delta_{\varphi})$ L_{Misal} for hovering displacements $\Delta_{\theta}, \Delta_{\varphi}$ L_{Δ_i} Loss caused by UAV displacement in i G Set of all possible combinations of Δ_i Ω Subset of C causing a given loss γ_{th} Threshold for stochastic loss estimation $Algorithm Parameters$ Measured power pair of beams k $w_k(\Delta_i)$ Confidence-cost weight, pair k , dimension i pow_k Measured power pair of beams k ts Time-stamped t_{sweep} Beam-sweeping time M Location samples collected during t_{sweep} H Mapping matrix $(pow_k, UAV_{x,y,z})$	L _{Afr}	UAV airframe-related loss
L_{SubOpt} Sub-optimal beam selection loss L_{Misal} Beam misalignment loss L_{Δ_r} Distance d fluctuation loss L_{Tot} Total link loss θ_T, φ_T Transmitter steering angles θ_T, φ_R Receiver steering angles $f_T(\theta), f_T(\varphi)$ Tx PDF to sweep in certain angle $f_R(\theta), f_R(\varphi)$ Rx PDF to sweep in certain angle $f_{R_{SW}}$ Tx steering PDF given beamforming $f_{R_{SW}}$ Rx steering PDF given beamforming u, v Candidate beams in θ and φ U, V Total candidate beams (u, v) N_b Total combination of candidate beams $L_{Tx}(\theta_u), L_{Tx}(\varphi_v)$ L_{SubOpt} at transmitter given pair (u, v) $L_{Tx}(\Delta_{\theta}), L_{Tx}(\Delta_{\varphi})$ L_{Misal} for hovering displacements $\Delta_{\theta}, \Delta_{\varphi}$ L_{Δ_i} Loss caused by UAV displacement in i C Set of all possible combinations of Δ_i Ω Subset of C causing a given loss γ_{th} Threshold for stochastic loss estimation $Algorithm Parameters$ Measured power pair of beams k ts Time-stamped t_{sweep} Beam-sweeping time M Location samples collected during t_{sweep} H Mapping matrix $(pow_k, UAV_{x,y,z})$ k^* Proposed pair of beams	L_{Hov}	Hovering-related loss
L_{Misal} Beam misalignment loss L_{Δ_r} Distance d fluctuation loss L_{Tot} Total link loss θ_T, φ_T Transmitter steering angles θ_R, φ_R Receiver steering angles $f_r(\theta), f_r(\varphi)$ Tx PDF to sweep in certain angle $f_R(\theta), f_R(\varphi)$ Rx PDF to sweep in certain angle $f_{r_{SW}}$ Tx steering PDF given beamforming $f_{R_{SW}}$ Rx steering PDF given beamforming u, v Candidate beam indices in θ and φ U, V Total candidate beams in θ and φ S Subset of candidate beams (u, v) N_b Total combination of candidate beams $L_{Tx}(\theta_u), L_{Tx}(\varphi_v)$ L_{SubOpt} at transmitter given pair (u, v) $L_{Tx}(\Delta_{\theta}), L_{Tx}(\Delta_{\varphi})$ L_{Misal} for hovering displacements $\Delta_{\theta}, \Delta_{\varphi}$ L_{Δ_i} Loss caused by UAV displacement in i C Set of all possible combinations of Δ_i Ω Subset of C causing a given loss γ_{th} Threshold for stochastic loss estimation $Algorithm Parameters$ Measured power pair of beams k ts Time-stamped t_{sweep} Beam-sweeping time M Location samples collected during t_{sweep} H Mapping matrix $(pow_k, UAV_{x,y,z})$ k^* Proposed pair of beams	L_{SubOpt}	Sub-optimal beam selection loss
$\begin{array}{lll} L_{\Delta_r} & \text{Distance d fluctuation loss} \\ L_{Tot} & \text{Total link loss} \\ \theta_T, \varphi_T & \text{Transmitter steering angles} \\ \theta_R, \varphi_R & \text{Receiver steering angles} \\ f_T(\theta), f_T(\varphi) & \text{Tx PDF to sweep in certain angle} \\ f_R(\theta), f_R(\varphi) & \text{Rx PDF to sweep in certain angle} \\ f_{rsw} & \text{Tx steering PDF given beamforming} \\ f_{rsw} & \text{Rx steering PDF given beamforming} \\ u, v & \text{Candidate beam indices in θ and φ \\ U, V & \text{Total candidate beams in θ and φ \\ S & \text{Subset of candidate beams (u, v) \\ N_b & \text{Total combination of candidate beams} \\ L_{Tx}(\theta_u), L_{Tx}(\varphi_v) & L_{SubOpt} \text{ at transmitter given pair (u, v) \\ L_{Tx}(\Delta_{\theta}), L_{Tx}(\Delta_{\varphi}) & L_{Misal} \text{ for hovering displacements $\Delta_{\theta}, \Delta_{\varphi}$ \\ L_{\Delta_i} & \text{Set of all possible combinations of Δ_i \\ \Omega & \text{Subset of C causing a given loss} \\ \gamma_{th} & \text{Threshold for stochastic loss estimation} \\ \hline Algorithm Parameters \\ \hline w_k(\Delta_i) & \text{Confidence weight, pair k, dimension i \\ pow_k & \text{Measured power pair of beams k \\ ts & \text{Time-stamped} \\ t_{sweep} & \text{Beam-sweeping time} \\ M & \text{Location samples collected during t_{sweep} \\ H & \text{Mapping matrix $(pow_k, UAV_{x,y,z})$ \\ k^* & \text{Proposed pair of beams $} \\ \hline \end{array}$	L_{Misal}	Beam misalignment loss
$\begin{array}{lll} L_{Tot} & \text{Iotal link loss} \\ \theta_{T}, \varphi_{T} & \text{Transmitter steering angles} \\ \theta_{R}, \varphi_{R} & \text{Receiver steering angles} \\ f_{f}(\theta), f_{T}(\varphi) & \text{Tx PDF to sweep in certain angle} \\ f_{R}(\theta), f_{R}(\varphi) & \text{Rx PDF to sweep in certain angle} \\ f_{r_{SW}} & \text{Tx steering PDF given beamforming} \\ f_{r_{SW}} & \text{Rx steering PDF given beamforming} \\ u, v & \text{Candidate beam indices in } \theta \text{ and } \varphi \\ U, V & \text{Total candidate beams in } \theta \text{ and } \varphi \\ S & \text{Subset of candidate beams } (u, v) \\ N_{b} & \text{Total combination of candidate beams} \\ L_{Tx}(\theta_{u}), L_{Tx}(\varphi_{v}) & L_{SubOpt} \text{ at transmitter given pair } (u, v) \\ L_{Tx}(\Delta_{\theta}), L_{Tx}(\Delta_{\varphi}) & L_{Misal} \text{ for hovering displacements } \Delta_{\theta}, \Delta_{\varphi} \\ L_{\Delta_{i}} & \text{Loss caused by UAV displacement in } i \\ C & \text{Set of all possible combinations of } \Delta_{i} \\ \Omega & \text{Subset of } C \text{ causing a given loss} \\ \gamma_{th} & \text{Threshold for stochastic loss estimation} \\ \hline Algorithm Parameters \\\hline w_{k}(\Delta_{i}) & \text{Confidence weight, pair } k, \text{ dimension } i \\ pow_{k} & \text{Measured power pair of beams } k \\ ts & \text{Time-stamped} \\ t_{sweep} & \text{Beam-sweeping time} \\ M & \text{Location samples collected during } t_{sweep} \\ H & \text{Mapping matrix } (pow_{k}, UAV_{x,y,z}) \\ k^{*} & \text{Proposed pair of beams} \\ \end{array}$	L_{Δ_r}	Distance d fluctuation loss
$\begin{array}{llllllllllllllllllllllllllllllllllll$	L_{Tot}	Total link loss
σ_R, φ_R Receiver steering angles $f_r(\theta), f_r(\varphi)$ Tx PDF to sweep in certain angle $f_R(\theta), f_R(\varphi)$ Rx PDF to sweep in certain angle $f_{r_{SW}}$ Tx steering PDF given beamforming $f_{r_{SW}}$ Rx steering PDF given beamforming u, v Candidate beam indices in θ and φ U, V Total candidate beams in θ and φ S Subset of candidate beams (u, v) N_b Total combination of candidate beams $L_{Tx}(\theta_u), L_{Tx}(\varphi_v)$ L_{SubOpt} at transmitter given pair (u, v) $L_{Tx}(\Delta_{\theta}), L_{Tx}(\Delta_{\varphi})$ L_{Misal} for hovering displacements $\Delta_{\theta}, \Delta_{\varphi}$ L_{Δ_i} Set of all possible combinations of Δ_i Ω Subset of C causing a given loss γ_{th} Threshold for stochastic loss estimationAlgorithm ParametersMeasured power pair of beams k $w_k(\Delta_i)$ Confidence weight, pair k , dimension i pow_k Measured power pair of beams k ts Time-stamped t_{sweep} Beam-sweeping time M Location samples collected during t_{sweep} H Mapping matrix $(pow_k, UAV_{x,y,z})$ k^* Proposed pair of beams	θ_T, φ_T	Transmitter steering angles
$f_{R}(\varphi), f_{R}(\varphi)$ for the sweep in certain angle $f_{R}(\theta), f_{R}(\varphi)$ Rx PDF to sweep in certain angle $f_{r_{SW}}$ Rx PDF to sweep in certain angle $f_{r_{SW}}$ Rx steering PDF given beamforming u, v Candidate beam indices in θ and φ U, V Total candidate beams in θ and φ S Subset of candidate beams (u, v) N_b Total combination of candidate beams $L_{Tx}(\theta_u), L_{Tx}(\varphi_v)$ L_{SubOpt} at transmitter given pair (u, v) L_{Δ_i} Cos caused by UAV displacements $\Delta_{\theta}, \Delta_{\varphi}$ C Set of all possible combinations of Δ_i Ω Subset of C causing a given loss γ_{th} Threshold for stochastic loss estimationAlgorithm ParametersWeasured power pair of beams k $w_k(\Delta_i)$ Confidence weight, pair k , dimension i pow_k Measured power pair of beams k ts Time-stamped t_{sweep} Beam-sweeping time M Location samples collected during t_{sweep} H Mapping matrix $(pow_k, UAV_{x,y,z})$ k^* Proposed pair of beams	ψ_R, ψ_R fr (A) fr (c)	Ty PDE to sween in certain angle
$\begin{array}{llllllllllllllllllllllllllllllllllll$	$f_{\mathbf{p}}(\theta), f_{\mathbf{r}}(\varphi)$	Rx PDF to sweep in certain angle
$\begin{array}{cccc} f_{R_{SW}} & Rx steering PDF given beamforming \\ f_{R_{SW}} & Rx steering PDF given beamforming \\ u,v & Candidate beam indices in \theta and \varphiU,V & Total candidate beams in \theta and \varphiS & Subset of candidate beams (u,v)N_b & Total combination of candidate beams \\ L_{Tx}(\theta_u), L_{Tx}(\varphi_v) & L_{SubOpt} at transmitter given pair (u,v)L_{Tx}(\Delta_{\theta}), L_{Tx}(\Delta_{\varphi}) & L_{SubOpt} at transmitter given pair (u,v)L_{\Delta_i} & Loss caused by UAV displacements \Delta_{\theta}, \Delta_{\varphi}L_{\Delta_i} & Set of all possible combinations of \Delta_i\Omega & Subset of C causing a given loss \\ \gamma_{th} & Threshold for stochastic loss estimation \\ \hline Algorithm Parameters & \\ w_k(\Delta_i) & Confidence weight, pair k, dimension i \\ pow_k & Measured power pair of beams k \\ ts & Time-stamped \\ t_{sweep} & Beam-sweeping time \\ M & Location samples collected during t_{sweep} \\ H & Mapping matrix (pow_k, UAV_{x,y,z}) \\ k^* & Proposed pair of beams \end{array}$	$f_{T-\dots}$	Tx steering PDF given beamforming
u, v Candidate beam indices in θ and φ u, v Total candidate beams in θ and φ U, V Total candidate beams in θ and φ S Subset of candidate beams (u, v) N_b Total combination of candidate beams $L_{Tx}(\theta_u), L_{Tx}(\varphi_v)$ L_{SubOpt} at transmitter given pair (u, v) L_{Δ_i} Loss caused by UAV displacements $\Delta_{\theta}, \Delta_{\varphi}$ C Set of all possible combinations of Δ_i Ω Subset of C causing a given loss γ_{th} Threshold for stochastic loss estimationAlgorithm ParametersConfidence weight, pair k , dimension i $w_k(\Delta_i)$ Confidence weight, pair k , dimension i pow_k Measured power pair of beams k ts Time-stamped t_{sweep} Beam-sweeping time M Location samples collected during t_{sweep} H Mapping matrix $(pow_k, UAV_{x,y,z})$ k^* Proposed pair of beams	f _{Rsw}	Rx steering PDF given beamforming
U, V Total candidate beams in θ and φ' S Subset of candidate beams (u, v) N_b Total combination of candidate beams $L_{Tx}(\theta_u), L_{Tx}(\varphi_v)$ L_{SubOpt} at transmitter given pair (u, v) L_{Δ_i} L_{SubOpt} at transmitter given pair (a, v) C Set of all possible combinations of Δ_i Ω Subset of C causing a given loss γ_{th} Threshold for stochastic loss estimationAlgorithm ParametersConfidence weight, pair k , dimension i $w_k(\Delta_i)$ Confidence cost weight, pair k , dimension i pow_k Measured power pair of beams k ts Time-stamped t_{sweep} Beam-sweeping time M Location samples collected during t_{sweep} H Mapping matrix $(pow_k, UAV_{x,y,z})$ k^* Proposed pair of beams	u, v	Candidate beam indices in θ and φ
SSubset of candidate beams (u, v) N_b Total combination of candidate beams $L_{Tx}(\theta_u), L_{Tx}(\varphi_v)$ L_{SubOpt} at transmitter given pair (u, v) $L_{Tx}(\Delta_{\theta}), L_{Tx}(\Delta_{\varphi})$ L_{Misal} for hovering displacements $\Delta_{\theta}, \Delta_{\varphi}$ L_{Δ_i} Loss caused by UAV displacement in i C Set of all possible combinations of Δ_i Ω Subset of C causing a given loss γ_{th} Threshold for stochastic loss estimationAlgorithm Parameters $W_k(\Delta_i)$ $w_k(\Delta_i)$ Confidence weight, pair k , dimension i pow_k Measured power pair of beams k ts Time-stamped t_{sweep} Beam-sweeping time M Location samples collected during t_{sweep} H Mapping matrix $(pow_k, UAV_{x,y,z})$ k^* Proposed pair of beams	U, V	Total candidate beams in θ and φ
$\begin{array}{lll} N_b & \mbox{Total combination of candidate beams} \\ L_{Tx}(\theta_u), L_{Tx}(\varphi_v) & L_{SubOpt} \mbox{ at transmitter given pair } (u, v) \\ L_{Tx}(\Delta_{\theta}), L_{Tx}(\Delta_{\varphi}) & \mbox{ L_{Misal} for hovering displacements } \Delta_{\theta}, \Delta_{\varphi} \\ L_{\Delta_i} & \mbox{ Loss caused by UAV displacement in } i \\ C & \mbox{ Set of all possible combinations of } \Delta_i \\ \Omega & \mbox{ Subset of } C \mbox{ causing a given loss } \\ \gamma_{th} & \mbox{ Threshold for stochastic loss estimation } \\ Algorithm Parameters & \\ \hline w_k(\Delta_i) & \mbox{ Confidence weight, pair } k, \mbox{ dimension } i \\ pow_k & \mbox{ Measured power pair of beams } k \\ ts & \mbox{ Time-stamped } \\ t_{sweep} & \mbox{ Beam-sweeping time } \\ M & \mbox{ Location samples collected during } t_{sweep} \\ H & \mbox{ Mapping matrix } (pow_k, UAV_{x,y,z}) \\ k^* & \mbox{ Proposed pair of beams } \end{array}$	S	Subset of candidate beams (u, v)
$\begin{array}{lll} L_{Tx}(\theta_u), L_{Tx}(\varphi_v) & L_{SubOpt} \text{ at transmitter given pair } (u,v) \\ L_{Tx}(\Delta_{\theta}), L_{Tx}(\Delta_{\varphi}) & L_{Misal} \text{ for hovering displacements } \Delta_{\theta}, \Delta_{\varphi} \\ L_{\Delta_i} & \text{Loss caused by UAV displacement in } i \\ \hline C & \text{Set of all possible combinations of } \Delta_i \\ \hline \Omega & \text{Subset of } C \text{ causing a given loss} \\ \hline \gamma_{th} & \text{Threshold for stochastic loss estimation} \\ \hline Algorithm Parameters & \\ \hline w_k(\Delta_i) & \text{Confidence weight, pair } k, \text{ dimension } i \\ \hline pow_k & \text{Measured power pair of beams } k \\ \hline ts & \text{Time-stamped} \\ \hline t_{sweep} & \text{Beam-sweeping time} \\ \hline M & \text{Location samples collected during } t_{sweep} \\ \hline H & \text{Mapping matrix } (pow_k, UAV_{x,y,z}) \\ k^* & \text{Proposed pair of beams} \end{array}$	N_b	Total combination of candidate beams
$\begin{array}{lll} L_{Tx}(\Delta_{\theta}), L_{Tx}(\Delta_{\varphi}) & L_{Misal} \text{ for hovering displacements } \Delta_{\theta}, \Delta_{\varphi} \\ L_{\Delta_i} & \text{Loss caused by UAV displacement in } i \\ C & \text{Set of all possible combinations of } \Delta_i \\ \Omega & \text{Subset of } C \text{ causing a given loss} \\ \hline \gamma_{th} & \text{Threshold for stochastic loss estimation} \\ \hline Algorithm Parameters & \\\hline w_k(\Delta_i) & \text{Confidence weight, pair } k, \text{ dimension } i \\ pow_k & \text{Measured power pair of beams } k \\ ts & \text{Time-stamped} \\ \hline t_{sweep} & \text{Beam-sweeping time} \\ M & \text{Location samples collected during } t_{sweep} \\ H & \text{Mapping matrix } (pow_k, UAV_{x,y,z}) \\ k^* & \text{Proposed pair of beams} \end{array}$	$L_{Tx}(\theta_u), L_{Tx}(\varphi_v)$	L_{SubOpt} at transmitter given pair (u, v)
L_{Δ_i} Loss caused by UAV displacement in i C Set of all possible combinations of Δ_i Ω Subset of C causing a given loss γ_{th} Threshold for stochastic loss estimationAlgorithm Parameters $w_k(\Delta_i)$ $w_k(\Delta_i)$ Confidence weight, pair k , dimension i pow_k Measured power pair of beams k ts Time-stamped t_{sweep} Beam-sweeping time M Location samples collected during t_{sweep} H Mapping matrix $(pow_k, UAV_{x,y,z})$ k^* Proposed pair of beams	$L_{Tx}(\Delta_{\theta}), L_{Tx}(\Delta_{\varphi})$	L_{Misal} for hovering displacements $\Delta_{\theta}, \Delta_{\varphi}$
CSet of all possible combinations of Δ_i Ω Subset of C causing a given loss γ_{th} Threshold for stochastic loss estimationAlgorithm Parameters $w_k(\Delta_i)$ $w_k(\Delta_i)$ Confidence weight, pair k, dimension i pow_k Measured power pair of beams k ts Time-stamped t_{sweep} Beam-sweeping timeMLocation samples collected during t_{sweep} HMapping matrix $(pow_k, UAV_{x,y,z})$ k^* Proposed pair of beams	L_{Δ_i}	Loss caused by UAV displacement in <i>i</i>
Σ Subset of C causing a given loss γ_{th} Threshold for stochastic loss estimationAlgorithm Parameters K $w_k(\Delta_i)$ Confidence weight, pair k, dimension i $w_{Lk}(\Delta_i)$ Confidence-cost weight, pair k, dimension i pow_k Measured power pair of beams k ts Time-stamped t_{sweep} Beam-sweeping timeMLocation samples collected during t_{sweep} HMapping matrix $(pow_k, UAV_{x,y,z})$ k^* Proposed pair of beams	C	Set of all possible combinations of Δ_i
γ_{th} Intresticit for stochastic loss estimationAlgorithm Parameters $w_k(\Delta_i)$ Confidence weight, pair k, dimension i $w_{L_k}(\Delta_i)$ Confidence-cost weight, pair k, dimension i pow_k Measured power pair of beams k ts Time-stamped t_{sweep} Beam-sweeping timeMLocation samples collected during t_{sweep} HMapping matrix $(pow_k, UAV_{x,y,z})$ k^* Proposed pair of beams	22	Subset of C causing a given loss
$w_k(\Delta_i)$ Confidence weight, pair k , dimension i $w_{L_k}(\Delta_i)$ Confidence-cost weight, pair k , dimension i pow_k Measured power pair of beams k ts Time-stamped t_{sweep} Beam-sweeping time M Location samples collected during t_{sweep} H Mapping matrix $(pow_k, UAV_{x,y,z})$ k^* Proposed pair of beams	Yth Algorithm Daventer	Threshold for slochastic loss estimation
$w_k(\Delta_i)$ Confidence weight, pair k, dimension l $w_{L_k}(\Delta_i)$ Confidence-cost weight, pair k, dimension i pow_k Measured power pair of beams k ts Time-stamped t_{sweep} Beam-sweeping timeMLocation samples collected during t_{sweep} HMapping matrix $(pow_k, UAV_{x,y,z})$ k^* Proposed pair of beams	Augorumm Purumeters	Confidence weight pair k dimension i
$w_{L_k}(x_l)$ Connected store weight, pair k, uniterision t pow_k Measured power pair of beams k ts Time-stamped t_{sweep} Beam-sweeping time M Location samples collected during t_{sweep} H Mapping matrix $(pow_k, UAV_{x,y,z})$ k^* Proposed pair of beams	$w_k(\Delta_i)$ $w_k(\Lambda_i)$	Confidence-cost weight pair k, dimension i
ts Time-stamped ts Time-stamped t_{sweep} Beam-sweeping time M Location samples collected during t_{sweep} H Mapping matrix $(pow_k, UAV_{x,y,z})$ k^* Proposed pair of beams	$w_{L_k}(\Delta_i)$	Measured power pair of hears l
t_{sweep} Beam-sweeping time M Location samples collected during t_{sweep} H Mapping matrix $(pow_k, UAV_{x,y,z})$ k^* Proposed pair of beams	POW_K	Time-stamped
M Location samples collected during t_{sweep} M Mapping matrix $(pow_k, UAV_{x,y,z})$ k^* Proposed pair of beams	tswaan	Beam-sweeping time
HMapping matrix $(pow_k, UAV_{x,y,z})$ k^* Proposed pair of beams	M	Location samples collected during tsween
k^* Proposed pair of beams	Н	Mapping matrix $(pow_k, UAV_{x,y,z})$
	k^*	Proposed pair of beams



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